

Foundational Numeracy





Working with Decimals

Introduction to Decimals

Decimals are similar to fractions as they are also used to represent parts of a whole



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- The price tag to the left reads **\$18.98**
- The number **18.98** is written in **decimal notation**
- A number written in decimal notation is often just called a **decimal**



Introduction to Decimals

Decimals are similar to fractions as they are also used to represent parts of a whole



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A number written as a **decimal** has 3 parts:

- 1. Whole Number Portion
- 2. Decimal Point
- 3. Decimal Portion (the numbers that come after the decimal point)



Decimals – Place Value is

18.98

Periods:	E	Billion	S	N	lillion	IS	Th	ousai	ıds		Ones	
PLACE VALUE:	Hundred-billions	Ten-billions	Billions	Hundred-millions	Ten-millions	Millions	Hundred-thousands	Ten-Thousands	Thousands	Hundreds	Tens	Ones
Example:												

If you recall, this is the place value chart we used for WHOLE NUMBERS on Day 1

Place names and place values for the whole number portion of a decimal number are exactly the same

Place names and place values for the decimal portion are similar, but move the opposite direction and end in suffix "ths"



Decimals – Place Value is

A number written as a **decimal** has 3 parts:

- 1. Whole Number Portion
- 2. Decimal Point
- 3. Decimal Portion (the numbers that come after the decimal point)





Step 1: Write/say the whole number portion in words

Step 2: Write/say "and" for the decimal point

Step 3: Write/say the decimal portion in words as though it were a whole number, followed by the place value of only the **last** digit of the decimal portion



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21.94 **"Twenty one and ninety four hundredths"**



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192.639 "One hundred ninety two and six hundred thirty nine thousandths"



Step 1: Write/say the whole number portion in words

Step 2: Write/say "and" for the decimal point

Step 3: Write/say the decimal portion in words as though it were a whole number, followed by the place value of only the **last** digit of the decimal portion



9729.4538

"Nine thousand, seven hundred twenty nine and four thousand five hundred thirty eight ten-thousandths"



The Golden Jubilee Diamond



Carats: 545.67 carats

- The largest cut and largest faceted diamond in the whole world
- Outweighs the 2nd largest diamond in the world (The Cullinan I) by 15.37 carats
- Approximate value in 2021: \$4-12 Million
- Discovered in 1985; bought by De Beers group in 1995
- Now displayed in the Royal Palace in Bangkok as part of the "Crown Jewels" of Thailand



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Step 1: Write/say the whole number portion in words

Step 2: Write/say "and" for the decimal point

Step 3: Write/say the decimal portion in words as though it were a whole number, followed by the place value of only the **last** digit of the decimal portion



545.67 **"Five hundred forty five and sixty seven hundredths"**



"Twenty one and eight hundred two thousandths"





"Six and ninety four ten-thousandths"





"Five and twenty five hundredths"





"Eight thousandths"





We round the decimal portion of a decimal number in nearly the same way as we round whole numbers

Rounding to the Nearest THOUSAND



The only difference:

For Whole numbers, we turn the digits to the right of the intended place value into 0's. Ex: Round 925 to the nearest **hundred** \rightarrow 900

For decimals, we simple *drop* the values to the right of the intended place value



1) Establish your intended place value \uparrow

2) Look to the right of your intended place value

- If the number to the right of your intended place value is less than 5, keep the digit in your intended place value the same

- If the number to the right of your intended place value is 5 or greater, increase the digit in your intended place value by 1

- IN BOTH SCENARIOS, be sure to **drop** all digits that come after your intended place value

Round 34.3617 to the nearest **tenth**

34.3617



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- IN BOTH SCENARIOS, be sure to **drop** all digits that come after your intended place value

Round 34.3617 to the nearest **thousandth**

34.3617



Converting Decimals into Fractions

Decimal	In Words	Fraction
0.1	"one tenth"	$\frac{1}{10}$
0.39	"thirty nine hundredths"	$\frac{39}{100}$
0.096	"ninety six thousandths"	$\frac{96}{1000}$
0.0008	"eight ten thousandths"	<u>8</u> 10,000



Converting Decimals into Fractions

Write each decimal as a fraction or a mixed number. Write your answers in *simplest form*.





Converting Decimals into Fractions

Write each decimal as a fraction or a mixed number. Write your answers in *simplest form*.

0.8 "eight tenths"	$\frac{8}{10}$
The Prime Factorization of the numerator : $2 \cdot 2 \cdot 2$	$\frac{2 \cdot 2 \cdot 2}{2 \cdot 5}$ $\frac{2 \cdot 2}{5}$
The Prime Factorization of the denominator : $2 \cdot 5$	$=\frac{4}{5}$



Mixed Numbers and Decimals: "AND"

Mixed Numbers and decimals are similar in that both use the word "AND" to separate the whole number portion from the part of a whole portion 6.5 3.75 23.625 "six and five tenths" "three and seventy five hundredths" "twenty three and six hundred twenty five thousandths" $3\frac{75}{100}$ $23\frac{625}{1000}$ $6\frac{5}{10}$ $6\frac{1}{2}$ $3\frac{3}{4}$ $23\frac{5}{8}$



"Write each fraction as a decimal"

We use long-division to convert fractions into decimals •

Up until this point, we have only performed long-division on fractions that look like this:

Now, we will perform long-division on fractions that look like this:

extra step before doing long-division



4 4 2 $2\frac{2}{4}$ or $2\frac{1}{2}$

"Write each fraction as a decimal"

For ANY decimal, inserting 0's after the last digit to the RIGHT of the decimal point does not change the value of the number

- Some questions will require you to add 2 decimal places to the numerator/dividend... sometimes you will need 3 decimal places...
- Keep dividing until you get a good picture of what the decimal will actually be

 To make the long division possible, we must add decimal places to our **numerator/dividend**

Place a decimal in the **quotient** directly above the decimal point of the **numerator/dividend**

Divide as per usual (ignore the decimal points for now)

"10 does not go into 4, but it does go into 40."



 $\frac{4}{10}$

10 4

"Write each fraction as a decimal"



 $\frac{375}{1000}$ in simplest form is $\frac{3}{8}$



Write each mixed number as a decimal:



What's going on here?





Operations on Decimals

Addition & Subtraction

Multiplication & Division

Extensions - comparing, rounding, converting, etc.





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The following information is based off Laps 13 and 14 for $\frac{5}{20}$ drivers during the 2021 Formula 1 Spanish Grand Prix that took place on Sunday, May 9th, 2021

Driver	Lap 13Lap 14(seconds)(seconds)
Lewis Hamilton	83.038 83.18
	84.619 84.666
Charles Leclerc	
Max Verstappen	83.038 83.155
Sebastian Vettel	85.487 85.315



1) Which driver was able to **improve** their lap time on the 14th lap in comparison to their previous lap?

Hamilton	83.038	<	83.18
Ricciardo	84.619	<	84.666
Leclerc	83.839	<	83.846
Verstappen	83.038	<	83.155
Vettel	85.487	>	85.315

∴ The only driver that was able to improve their lap time on the 14th lap in comparison to their previous lap was Sebastian Vettel

rix	Lap 13	Lap 14
Driver	(seconds)	(seconds)
Lewis Hamilton	83.038	83.18
Daniel Ricciardo	84.619	84.666
Charles Leclerc	83.839	83.846
Max Verstappen	83.038	83.155
Sebastian Vettel	85.487	85.315



2) How much better did Sebastian Vettel do in lap 14 in comparison to lap 13? Round your answer to the nearest tenth.

We have to find the difference! Subtraction

When adding or subtracting decimals, write your numbers so that the decimal points and all place values line up vertically

Then, add or subtract as with whole numbers! Line up decimal in sum/difference

85.487 85.315 00.172 **0.2**

 \therefore Sebastian Vettel was able to improve his 14th lap time by 0.2 seconds (two tenths of a second)

	Lap 13	Lap 14
Driver		
Lewis Hamilton	83.038	83.18
Daniel Ricciardo	84.619	84.666
Charles Leclerc	83.839	83.846
Max Verstappen	83.038	83.155
Sebastian Vettel	85.487	85.315



3) What was Lewis Hamilton's combined time for both laps? Round your answer to the nearest hundredth.

Combined means: Addition

When adding or subtracting decimals, write your numbers so that the decimal points and all place values line up vertically

Then, add or subtract as with whole numbers! Line up decimal in sum/difference

 $1 \\ 83.180 \\ + 83.038 \\ 166.218 \\ = 166.22$

∴ Lewis Hamilton's combined time for both laps 13 and 14 is 166.22 seconds

'rix	Lap 13	Lap 14
Driver	(seconds)	(seconds)
Lewis Hamilton	83.038	83.18
Daniel Ricciardo	84.619	84.666
Charles Leclerc	83.839	83.846
Max Verstappen	83.038	83.155
Sebastian Vettel	85.487	85.315



4) Calculate ea	ch driver's combined lap times. Then, rank ea	ch Driv	/er	Lap 13 (seconds)	Lap 14 (seconds)
driver from <u>fas</u> race.	test to slowest at this specific interval of the				
Hamilton	Verstappen	Lewis Hamilton		83.038	83.18
1	1		The minute by unknown Author is likensed under a datability		
83.180	83.155				
+ 83.038	+ 83.038	Daniel Ricciardo	The Rings by Unknown Author is licensed under <u>CC BV-NC</u>	84.619	84.666
166.218	166.193				
Leclerc	Ricciardo	Charles Leclerc		83.839	83.846
1 1 83.846 + 83.839 167.685	84.666 + <u>84.619</u> 169.285	Max Verstappen	RECEVENCE AND CONSTRUCTIONS	83.038	83.155
-	Vettel 1 11 85.315 + 85.487	Sebastian Vettel	ASTON MARTIN Cognizant FORMULA ONE-TEAM	85.487	85.315
	170.802				



4) Calculate each driver's combined lap times. Then, rank each driver from <u>fastest to slowest</u> at this specific interval of the race.

Hamilton: 166.218 seconds

Ricciardo: 169.285 seconds

Leclerc: 167.685 seconds

Verstappen: 166.193 seconds

Vettel: 170.802 seconds

- \therefore After calculating each driver's combined lap times in this specific interval, the ranking of each driver from <u>fastest to slowest</u> is:
 - 1. Verstappen (166.193 seconds)
 - 2. Hamilton (166.218 seconds)
 - 3. Leclerc (167.685 seconds)
 - 4. Ricciardo (169.285 seconds)
 - 5. Vettel (170.802 seconds)

Driver	Lap 13 (seconds)	Lap 14 (seconds)
Lewis Hamilton	83.038	83.18
Daniel Ricciardo	84.619	84.666
Charles Leclerc	83.839	83.846
Max Verstappen	83.038	83.155
Sebastian Vettel	85.487	85.315



Multiply.

 0.03×0.3

IF WE WERE TO CONVERT TO FRACTIONS FIRST ...

$\frac{3}{100} \times \frac{3}{10}$	
$\frac{3\cdot 3}{100\cdot 10}$	Is there a way to multiply decimals without converting to fractions first?
$\frac{9}{1000}$	Yes!
= 0.009	
$\therefore 0.03 \times 0.3 = 0.009$	



(which in this case, is 3)

Multiply.	0.03×0.3	
We do not have to convert these decimals to fractions in order to multiply them.	3 × 3	
To multiply decimals,	9	
Step 1: Multiply the decimals as if they were whole numbers	Factor 1: 0.03	2 decimal places
Step 2: The decimal point of the final product is placed so that the number of decimal places in the product is equal to the <i>sum</i> of the number of decimal places in each original factor	Factor 2: 0.3	+ <u>1</u> decimal places 3 total decimal places
Step 3: Starting from the right of your modified product (which in this case is 9), move the decimal place to the left the same amount of total decimal places calculated in Step 2	9 11	

Multiply.	0.03×0.3
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To multiply decimals,	9
Step 1: Multiply the decimals as if they were whole numbers	Factor 1: 0.03 2 decimal places
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Step 3: Starting from the right of your modified product (which in this case is 9), move the decimal place to the left the same amount of total decimal places calculated in Step 2 (which in this case, is 3)	$ \begin{array}{c} 0 & 0 & 0 & 9 \\ \hline 0 & 0.03 \times 0.3 = 0.009 \end{array} $



Multiply.

We do not have to convert these decimals to fractions in order to multiply them.

To multiply decimals,

Step 1: Multiply the decimals as if they were whole numbers

Step 2: The decimal point of the product is placed so that the number of decimal places in the product is equal to the *sum* of the number of decimal places in each original factor

Step 3: Starting from the **right** of your modified product, move the decimal place to the left the same amount of total decimal places calculated in Step 2 $\begin{array}{r}1\\24\\326\\\times 28\\\underline{2608}\\+652\\9128\end{array}$

 32.6×0.28

9128.

Factor 1: 32.6 1 decimal places Factor 2: 0.28 $+ \frac{2 \text{ decimal places}}{3 \text{ total decimal places}}$



Multiply.

We do not have to convert these decimals to fractions in order to multiply them.

To multiply decimals,

Step 1: Multiply the decimals as if they were whole numbers

Step 2: The decimal point of the product is placed so that the number of decimal places in the product is equal to the *sum* of the number of decimal places in each original factor

Step 3: Starting from the **right** of your modified product, move the decimal place to the left the same amount of total decimal places calculated in Step 2

1 24 326 28		
$^{1}\overline{2608}$ + <u>652</u>		
9128		

 32.6×0.28

9.128

 $\therefore 32.6 \times 0.28 = 9.128$

			3 total decimal places
Factor 2:	0.28	+_	2 decimal places
Factor 1:	32.6		1 decimal places



Multiplying by factors of 10 (10, 100, 1000, etc.)

When you multiply by a factor of 10, the decimal simply moves to the **right**.

If you multiply by 10, the decimal moves one place value.

If you multiply by 100, the decimal moves two places.

An easy way to remember this is to **count the number of zeroes**. If the number is multiplied by 100,000, that means that the decimal moves to the right 5 places.

Using "1" as an example:

Multiplication Form	Decimal Moves	Standard Form
1 × 1	None	1
1 × 10	1 to the right	10
1 × 100	2 to the right	100
1 × 1000	3 to the right	1000
1 × 10,000	4 to the right	10,000
1 × 100,000	5 to the right	100,000
1 × 1,000,000	6 to the right	1,000,000
1 × 10,000,000	7 to the right	10,000,000

Using "4.53962" as an example:

Multiplication Form	Decimal Moves	Standard Form
4.53962×1	None	4.53962
4.53962×10	1 to the right	45.3962
4.53962×100	2 to the right	453.962
4.53962×1000	3 to the right	4539.62
4.53962 × 10,000	4 to the right	45,396.2
4.53962 × 100,000	5 to the right	453,962
4.53962 × 1,000,000	6 to the right	4,539,620
4.53962 × 10,000,000	7 to the right	45,396,200



Dividing Decimals

With division and decimals, you will see these 2 kinds of questions:





Dividing by a Whole Number

1) Place the decimal point in the quotient directly above the decimal point in the numerator/dividend

This should be familiar: you've done this exact thing when converting fractions to decimals!



2) Divide as per usual

 $270.2 \div 7$ 270.2 7 38.6 0.260 56

\therefore 270.2 \div 7 = **38.6**



Dividing by a Whole Number

1) Place the decimal point in the $6.195 \div 15$ quotient directly above the decimal point in the numerator/dividend 6.195 This should be familiar: you've done this 15 exact thing when converting fractions to decimals! **Converting Fractions into Decimals** "Write each fraction as a decimal" .413 83 6.195 15 $\begin{array}{r}
 .375 \\
 8 \overline{)3.000} \\
 -24 \\
 -60 \\
 -56 \\
 -40 \\
 -40 \\
 0
 \end{array}$ = 0.37560 Note: 0.375 → "three hundred seventy five thousandths" is literally $\frac{375}{1000}$ 375 in simplest form is 19 \therefore 6.195 \div 15 = 0.413 _ 15 2) Divide as per usual 45

45



Dividing by a Decimal

2.3 is now a whole number at $\mathbf{23}$

(by moving decimal point 1 spot to the right)

10.764 is now **107.64**

1) Move the decimal point of the denominator/divisor to the right until the denominator/divisor is a whole number

2) Move the decimal point in the numerator/dividend to the right the same number of places as the decimal

decimal 1 spot to the right for the

point was moved in Step 1

numerator/dividend

10.764

 $10.764 \div 2.3$

10.764 2.3

2.3 10.764

4.68 07.64 92 156 $\therefore 107.64 \div 2.3 = 4.68$ $_{-}138$ 184 $_{-}184$ (by moving decimal point 1 spot to the right)

3) Divide as per usual with your new numbers

Since we moved the decimal 1 spot to the right in

the denominator/divisor, we must also move the



Dividing by a Decimal

1) Move the decimal point of the denominator/divisor to the right until the denominator/divisor is a whole number



 $0.32\,$ is now a whole number at $32\,$ (by moving decimal point 2 spots to the right)

2) Move the decimal point in the numerator/dividend to the right the same number of places as the decimal point was moved in Step 1

Since we moved the decimal 2 spots to the right in the denominator/divisor, we must also move the decimal 2 spots to the right for the numerator/dividend

5.264

 $5.264 \ \text{is now} \ \textbf{526.4} \\ \text{(by moving decimal point 2 spots to the right)}$

 $5.264 \div 0.32$ <u>5.264</u>

0.32

0.32 5.264

16.4 526.4 32 206192 144 128 16

Part of the dividend still exists... what do we do?



3) Divide as per usual with your new numbers

Dividing by a Decimal

1) Move the decimal point of the denominator/divisor to the right until the denominator/divisor is a whole number

 $5.264 \div 0.32$ <u>5.264</u>

0.32

0.32 5.264

16.45 0.32 0.32 is now a whole number at $\mathbf{32}$ 32 526.40 (by moving decimal point 2 spots to the right) 206 2) Move the decimal point in the numerator/dividend to the right the 192 same number of places as the decimal point was moved in Step 1 144Since we moved the decimal 2 spots to the right in $\therefore 5.264 \div 0.32 = 16.45$ the denominator/divisor, we must also move the $_{-}128$ decimal 2 spots to the right for the numerator/dividend 1605.264 5.264 is now **526.4** 160 (by moving decimal point 2 spots to the right)

3) Divide as per usual with your new numbers



Michael is a young man who is currently enrolled in NorQuest College's Cannabis Trimming & Production Online Course.

As part of his studies, **Michael** and a few of his classmates have decided to take a tour of Aurora Cannabis' production facility in Edmonton. They all hope to gain an understanding of how their studies can translate into careers through real world experience.



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TO ITEM



Cannabis Trimming & Production: online course







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During his tour of Aurora's massive 800,000 sq. ft production facility, **Michael** is intently watching one of the many technicians trim and package cannabis. The technician notices **Michael's** interest, and actually calls upon him to help him at his work station.





AURORA



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"During Aurora's packaging process, I have to ensure that each of these little childproof containers (exactly like the ones shown on the right) contains 3.5g of cannabis.

How many total (3.5g) containers will I be able to produce if I have 28g of trimmed, ready-for-packaging, cannabis?"

- Read the problem multiply times to familiarize yourself with the question
- 2) Collect evidence / organize thoughts
- 3) Build your equation
- 4) Solve and ANSWER



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"During Aurora's packaging process, I have to ensure that each of these little childproof containers (exactly like the ones shown on the right) contains 3.5g of cannabis.

How many total (3.5g) containers will I be able to produce if I have 28g of trimmed, ready-for-packaging, cannabis?"

Collect Evidence / Organize Thoughts

- 28g of "loose" cannabis
- Each container must contain 3.5g of cannabis
- How many containers?



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"During Aurora's packaging process, I have to ensure that each of these little childproof containers (exactly like the ones shown on the right) contains 3.5g of cannabis.

How many total (3.5g) containers will I be able to produce if I have 28g of trimmed, ready-for-packaging, cannabis?"



: With 28g, you would produce 8 total containers if each one carries 3.5g



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