# Foundational Numeracy



# Module 6: Integers, including Fractions and Decimals

Facilitator Guide

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## **Introduction to the Module**

In this module, you will solve numerical expressions using the order of operations. You will also explore signed numbers and practise solving numerical expressions with negative and positive numbers. Enjoy your studies!

#### Important

When you see an object like the one below, you can use a QR code scanner on your phone or tablet, and it will play a video of the math example. You can click on the link if you are working on a computer.



Want to watch a video of this lesson? Scan the QR Code to the left, or use the link below: <u>https://youtu.be/Hlal9ME2Aig</u>

# Note: The facilitator guide mirrors the Learner Guide with a couple of key differences.

- Facilitator notes throughout the module in boxes like this. Include teaching strategies and common errors
- Student Practice doesn't have this bubble. Instructor led The instructor can teach the concept or the learner can watch the video

## **Specific Learning Outcomes**

The table below displays the skills and knowledge you will explore in this module. This is your opportunity to evaluate your own skills to see if you can do these things. At the end of this module, you will be invited to re-evaluate your skills to measure the progress you have made.

	In this module, I will learn how to	I can't do this	I can do this with help	I can do this!
1.	Solve numerical expressions with negative and positive numbers			
2.	Solve numerical expressions using the order of operations			

## **Essential Skills**

The following essential skills are used in this module:



Reading: Understanding materials written in sentences or paragraphs



Numeracy: Using and understanding numbers



**Computer use/digital technology:** Using computers and other tools such as calculators and phones



Vocabulary: Gaining related vocabulary



**Thinking:** Finding information, problem solving, decision making, using your memory, planning job tasks and being organized, critical thinking

## **Unit 1: Introduction to Signed Numbers**

## Think about ...

- ♦ What is a negative number?
- What is the difference between  $-20^{\circ}$ C and  $20^{\circ}$ C?

## Keywords

Integer	Are positive and negative whole numbers
Negative whole numbers	Numbers less than zero, such as $-1, -2, -3, \dots$
Positive whole numbers	Numbers greater than zero, such as 1, 2, 3,
Opposites	Are numbers that are on the opposite side, but the same distance from zero.

## Integers

**Introductory Video** 



Numbers such as 1, 2, 3 ..., sometimes written +1, +2, +3 ..., are called **positive whole numbers**.

Numbers such as -1, -2, -3 ... are called **negative whole numbers**. The two sets together make the set of **integers**.

Integers are used in our daily lives and there are plenty of real world examples. Temperatures can be above freezing (positive) or below freezing (negative). In Alberta, it is common to have temperatures of  $+20^{\circ}$ C ( $20^{\circ}$ C) in the summer months. In the winter it is common to have temperatures  $-15^{\circ}$  C. Positive numbers can be written in two ways. We say 5, or +5. Numbers without signs are always positive.

Negative numbers can only be written in one way, -5.

### **Exercise 1.1**

Write the following using positive and negative numbers. If the number is positive, show it in two ways.

1.	A loss of \$500	
2.	A gain of 300 feet	
3.	A decrease of 7 pounds	
4.	An increase of 3 inches	
5.	A decrease of 20%	
6.	7 cars fewer	
7.	\$50 more	
8.	Down 30 metres	
9.	A gain of 7000 feet	
10.	A loss of 12 yards	

## **Integers on a Number Line**

Opposites are on opposite sides but the same distance from zero. There are many opposites in everyday life that use integers to describe them. Temperatures can be above freezing (positive) or below freezing (negative). Directions to the left are negative, whereas directions to the right are positive. In land elevations, positive integers indicate elevations above sea level, while negative integers indicate elevations below sea level.

Integers can be represented on a number line.

		I			1	I	1	1	1	
-4	-3	-2	-1	0	1	2	3	4	5	

Integers to the right are larger in value. Integers to the left are smaller in value. For example, -2 is greater than -4.

#### **Example:**

Arrange the integers -4, 6, 0, -7 in order from smallest to largest.

**Answer:** -7, -4, 0, 6

A number line is like a thermometer turned sideways.



Zero is neither negative nor positive.

## **Absolute Value**

Absolute value is always positive. Absolute value brackets also work as brackets, therefore solve inside bracket before changing to a positive values. Example |3 - 5| = |-2| = 2 or +2We use absolute values when adding and subtracting integers. Learners will see this video <u>https://youtu.be/oydj9zMLjIE</u>

The absolute value of a number is its distance from zero. The absolute value of a number is always positive. Absolute value brackets look like | |

The absolute value of |2| is 2 and |-2| is 2. Place them both on the number line.

-5 -4 -3 -2 -1 0 1 2 3 4 5

Notice that 2 and -2 are both 2 units from zero. These numbers are called opposites as they are the same distance from but on opposite sides of zero.

**Student practice:** 

Instructor led

1. Put the following numbers in order from smallest to largest.

-24, -30, -7, -10, -40

Scan the QR Code to the left, or use the link below: https://youtu.be/OvD5dXmDBc4

Find the absolute value of each of the following:

2. |-3|

3. |7|

4. |8-12|



Scan the QR Code to the left, or use the link below: https://youtu.be/frBJEYvyd-8

### Exercise 1.2

1. Graph each number on the number line by circling the number.



2. Write < or > between each pair of numbers to make a true statement. Remember that > means greater than and < means less than

a.	0	_ 2	b.	14
c.	_4		d.	-72
e.	-8	_ 2	f.	_47
g.	_5	5	h.	412
i.	-14	7	j.	-824

- 3. Write the absolute value of each of the following.
  - a. |-8| b. |0|
  - c. |15| d. |-37|
  - e. |-218| f. |45|

# Unit 2: Addition and Subtraction of Integers

## Keywords

<i>Like</i> signs	Signs that are the same
Unlike signs	Signs that are opposite
Subtracting integers	Add the opposite of the second number

## **Adding Integers**

When teaching adding integers focus learners on the idea that when signs are the same the numbers get larger but the sign stays the same. Example (-1) + (-2) = -3

Think 1 + 2 = 3 both signs are negative, therefore the answer the answer will be negative.

When signs are opposite we really subtract. The largest number will keep the sign This is where absolute values are important

Example (+2) + (-5) = -3 Think largest digit minus smallest digit.

In this case we think 5-2=3 Answer is -3 because largest number is negative therefore the answer will negative. Answer is -3

Common errors students make is not know which sign the answer should be.

When there are more than two numbers it is important to understand that we can add numbers in any order. As learners will tend to make less mistakes when they add than when they subtract we can add like signs together first.

(-16) + (+19) + (-10) + (+4) = first rewrite the numbers in a different order

(-16) + (-10) + (+19) + (+4) = add negatives then add positives

(-26) + (+23) notice now there is only one subtraction to do

Think 26 - 23 = 3 largest number was negative therefore the answer is negative. -3

Learner sees intro video https://youtu.be/\_BgblvF90UE

Study the following examples:

1. Add using a number line: (+2) + (+3)



Start at +2. Move 3 units to the **right** because 3 is positive (+3).

Answer: +5

2. Add using a number line: (-1) + (-2)



Start at -1. Move 2 units to the **left** because 2 is negative (-2).



3. (+2) + (-3)



Start at +2. Move 3 units to the **left** because 3 is negative (-3). **Answer:** -1

4. 
$$(-3) + (+4)$$



Start at –3. Move 4 units to the **right** because 4 is positive (+4).

#### Answer: +1

5. (+4) + (-5) + (+6) + (-3)

Add the positives first, then the negatives.

$$= (+4) + (+6) + (-5) + (-3)$$
$$= (+10) + (-8)$$
$$= +2$$

**Student practice:** 



Add and subtract using a number line.

1. 2 + -3 =



2. -2 + -3 =



3. -2 + 3 =



### **Summary of Addition Rules**

#### When signs are the same ...

Add the absolute values of the numbers and the signs stay the same.

- **Positive + Positive = Positive** 5+4=9
- Negative + Negative = Negative (-7) + (-2) = -9

#### When signs are opposite or unlike ...

Subtract the absolute values. The larger number keeps the sign.

- **Negative** + **Positive:** Use absolute values and subtract the smaller number from the larger one. The result takes the sign of the larger number.
  - (-7) + 4 = |-7| + |4| = 7 4 = 3, so -3 is your answer
  - 6 + (-9) = -3
  - (-3) + 7 = 4
  - 5 + (-3) = 2

Scan the QR Code to the left, or use the link below: https://youtu.be/NQSN00zL5gg **Student practice:** 



1. -15 + (-46) + (-29) =

Scan the QR Code to the left, or use the link below: <u>https://youtu.be/j3ty\_c9Fulg</u>

2. 15 + (-46) + 29 =

Scan the QR Code to the left, or use the link below: https://youtu.be/NrVvu7cM8\_o

### Exercise 2.1

- 1. (+6) + (+2) = 2. (+7) + (+10) =
- 3. (-8) + (-6) = 4. (-2) + (-3) =
- 5. -9 + -5 = 6. -12 + -7 =
- 7. (+70) + (+30) = 8. -16 + (+26) =
- 9. 134 + (-256) = 10. -169 + -234 =

11. (+16) + (-26) = 12. -12 + 25 =

13. 
$$(-18) + (+7) =$$
 14.  $(34) + (-29) =$ 

15. 
$$(+19) + (-47) + (-13) =$$
 16.  $(-16) + (+19) + (-10) =$ 

17. 
$$(-12) + (+15) + (-34) + (+12) =$$
 18.  $(+24) + (-5) + (-30) + (+17) =$ 

19. 
$$-22 + (+17) + (-34) + (+12) + (+8) + 34 =$$

20. 
$$12 + (-15) + (-27) + (+3) + (-11) + (+13) + (-14) =$$

## Subtracting Integers

Subtracting only has one more step than adding.

Never subtract, add the opposite of the second number.

(-6) - (+8) = we talk about two pen strokes as we change subtract to add change the sign of the to the number behind (-6) + (-8) = now we can add

Think 6 + 8 = 14 both are negative so the answer is -14

Common Error: changing subtract to add but not changing sign to the number

Learner will see introductory video https://youtu.be/c81Bg7ou6C4

Subtraction means changing the subtraction sign (-) to the addition sign (+), and changing the sign of the number behind it. This is known as "adding the opposite."

Study the following examples:

1. (+2) - (+5)

Start at +2. Change the direction to -5 (with integers, subtraction means to add the opposite). Move 5 units to the **left** to **add**.

Answer: -3

Or: 
$$(+2) - (+5) = (+2) + (-5) = -3 \leftarrow \text{Add the opposite}$$

Start at -4. Change the direction to +6. Move 6 units to the **right** to **add**.

**Answer:** 2 or +2

Or: 
$$(-4) - (-6) = (-4) + (+6) = +2$$

3. 
$$(+6) + (-5) - (+3) - (-7)$$

 $= (+6) + (-5) + (-3) + (+7) \leftarrow$  Change the subtraction to addition and change the signs to their opposite.

$$= (+6) + (+7) + (-5) + (-3) \quad \leftarrow \text{ Add the positives, then add the negatives.}$$
$$= (+13) + (-8)$$
$$= +5$$

Note: Addition signs followed by brackets can be dropped. (+6) + (-5) + (-3) + (+7) can be written as 6 - 5 - 3 + 7

4. Rewrite (-4) + (+10) - (+5) - (+2) without addition signs and brackets, then simplify.

= (-4) + (+10) + (-5) + (+2)= -4 + 10 - 5 + 2= -9 + 12= 3

### **Summary of Subtraction Rules**

When subtracting integers, add the first number to the **opposite** of the second number.

Change the subtraction sign to an addition sign, and change the sign of the following number to its opposite.

Remember, if the number doesn't have a sign, the number is positive.

#### Never subtract—always add the opposite

- Negative Positive = Negative (-5) 3 = -5 + (-3) = -8
- **Positive Negative = Positive + Positive = Positive** 5 (-3) = 5 + 3 = 8
- Negative Negative = Negative + Positive
   Use the sign of the larger number and subtract. (Change double negatives to a positive.)
   (-5) (-3) = (-5) + 3 = -2
   (-3) (-5) = (-3) + 5 = 2

#### **Student practice:**



Solve the following numerical expressions by both using a number line and without using a number line.



1. 2 - 3 =-5 -4 -3 -2 -1 0 1 2 3 4 5 2. -2 - 3 =-5 -4 -3 -2 -1 0 1 2 3 4 5 3. -2 + 3 =-5 -4 -3 -2 -1 0 1 2 3 4 5 4. -2 - (-3) =-5 -4 -3 -2 -1 0 1 2 3 4 5 5. 2-5 =-5 -4 -3 -2 -1 0 1 2 3 4 5 6. -3 - (-7) =-5 -4 -3 -2 -1 0 1 2 3 4 5

### **Exercise 2.2**

Solve the following numerical expressions.

- 1. (-1) (+2) =2. (+3) - (+5) =3. (-7) - (+10) =4. (-12) - (-8) =
- 5. (-5) (-2) = 6. (+7) (+10) =
- 7. (-6) (+8) = 8. (+16) (-16) =
- 9. (-16) (-16) = 10. 23 (-35) =
- 11. -72 (-29) = 12. -5 (+37) =
- 13. (-27) (+25) (-15) = 14. (+11) (-25) (+13) =

15. 
$$(-12) - (+15) + (-34) - (-12) =$$
 16.  $(-16) - (+5) - (-30) - (-12) =$ 

## **Problem Solving with Integers**

## **Tips for Solving Application Problems**

Read the tips below on solving application problems.

- Step 1: Read the question carefully. Read the problem several times.
- Step 2: Work out a plan and write an equation to solve the problem.
- Step 3: Estimate. Is your answer reasonable?
- **Step 4:** Solve the problem. Is your answer reasonable?
- **Step 5:** Write a statement.

#### Words that can be used to identify operations:

Addition	Subtraction	Equals
sum	difference	is
total	minus	is the same as
increased by	less than	equals
plus	more than	equal to
added to	decrease	results in
more	loss	
gain	fewer	

### **Exercise 2.3**

- 1. The temperature was 3°C at midday. By evening, the temperature was -5°C. What was the change in temperature?
- 2. A football team has to gain at least 10 yards (yds.) during four plays to keep the ball. Suppose that on four plays a team lost 6 yds., gained 8 yds., lost 2 yds., and gained 7 yds. Did the team gain enough yards to keep the ball?

3. On Monday, Jim had \$125 in his bank account. He deposited \$78, and paid bills of \$33 and \$142. How much money is left in his bank account?

- 4. The temperature was -7°C at midnight. By the next day, the temperature had risen by 11°C. What was the temperature the next day?
- At 8:00 a.m., the temperature was -18 degrees C. By 10:00 a.m., the temperature was 2 degrees C higher, and by 2:00 p.m., it had increased by another 4 degrees C. By 7:00 p.m., the temperature had dropped 13 degrees C. What was the temperature at 7:00 p.m.?

## Unit 3: Multiplication and Division of Signed Numbers

## Think about...

◆ How do you multiply and divide negative and positive numbers?

## **Keywords**

Integer	A number that is written without a fractional component; it can be positive or negative
Product	The answer when two or more numbers are multiplied together
Quotient	The answer when one number is divided by another

## **Multiplying Integers**

Have learners think about signs first. If there are odd number of negative signs the answer is negative. If there are even number of negatives the answer will be positive. Example  $(-4) \times (+2) \times (-3) = 2$  negative signs the answer is positive. Now can multiply numbers in any order 4x2x3 = +24Example  $(-4) \times (-2) \times (-3) = 3$  negatives answer is negative 4x2x3 = -24Learner sees intro video <u>https://youtu.be/K\_tPbVPfHgk</u>

The product of two integers with *like* signs is positive.

 $(+4) \times (+5) = +20$   $(-4) \times (-5) = +20$ 

The product of two integers with *unlike* signs is negative.

$$(+4) \times (-3) = -12$$
  $(-4) \times (+3) = -12$ 

Study the following examples.

1.  $(-4) \times (+2) \times (-3) \leftarrow$  Multiply the first two factors

 $= (-8) \times (-3)$ 

=+24

**Note:** If there is an **even** number of **negative factors**, the product will always be **positive**. (In this example, there were two negative factors, so the product was positive.)

If there is an **odd** number of **negative factors**, the product is **negative**.

2.  $(-3) \times (+5) \times (-2) \times (-1)$ 

=(-30)  $\leftarrow$  There are three negative factors (an odd number), so the product will be **negative**.

When brackets are together, it means to multiply. Therefore, example 2 can also be written as

(-3)(+5)(-2)(-1) = -30

This will become especially important when you start working with formulas. For example, the area of a square is calculated as  $Area = Length \times Width$  but this is most often written as A = LW. (When working with formulas, the brackets are implied.)

When you see brackets together, multiply!

### **Summary of Multiplication Rules**

<b>Positive</b> × <b>Positive</b> = <b>Positive</b>	$3 \times 2 = 6$
Negative × Negative = Positive	$(-2) \times (-8) = 16$
<b>Negative</b> × <b>Positive</b> = <b>Negative</b>	$(-3) \times 4 = -12$
<b>Positive</b> × <b>Negative</b> = <b>Negative</b>	$3 \times (-4) = -12$
Brackets together means to multiply	(3)(4) = 12
	Positive × Positive = Positive Negative × Negative = Positive Negative × Positive = Negative Positive × Negative = Negative Brackets together means to multiply

 Student practice:
 Instructor led

 1.  $2 \times 3 =$  Scan the QR Code to the left, or use the link below:

 https://youtu.be/47wjld9k2Hs

- 2.  $-2 \times 3 =$
- 3.  $2 \times -3 =$
- 4.  $-2 \times 3 =$

## Exercise 3.1

Solve the following numerical expressions.

1.  $(-5) \times 2 =$ 2.  $8 \times (-6) =$ 3.  $(-2) \times 8 =$ 4.  $2 \times (-7) =$ 5. (-1)(-7) = 6.  $(-6) \times 3 =$ 7. (+7)(-9) =8.  $6 \times (-8) =$ 9. (-7)(7) =10. (-7)(-8) =11. (-4)(+6) =12.  $70 \times (-8) =$ 13. (-8)(-8) =14. (-6)(+9) =15.  $-30 \times |-7| =$ 16. (-50)(-8) =17. (-7)(+4)(-2) =18. (-5)(-6)(-8) =19. (-8)(10) =20. (-10)(-6)(9) =

## Powers, Exponents, and Square Roots of Signed Numbers

A common error with exponents student will multiply the number with the exponent Example  $4^3 4x^3 = 12$  instead of multiplying the number with itself 3 times 4x4x4 = 64With negative numbers students get confused when the answer should be positive or negative

## Keywords

Power	The base and exponent together; for example $4^2$ , is a power and means $4 \times 4$
Base	The number the exponent is attached to; in the power $4^2$ , the base is <b>4</b>
Exponent	The number attached to the base that tells you how many times the base is multiplied with itself; in the power $4^2$ , the exponent is <b>2</b>
Square root	The opposite of squaring a number. The number in the square root sign, or <i>radical</i> , is a product of a number multiplied with itself; for example $\sqrt{16} = \sqrt{4 \times 4} = 4$ which means that <b>4 is the square root of 16</b>

### **Powers**

When the same factor is repeated or multiplied by itself, write the question as a power.

#### Examples:

- 1.  $(2)(2)(2)(2) = 2^4$  2 is the base, 4 is the exponent
- 2.  $(-3)(-3)(-3)(-3)(-3) = (-3)^5$  -3 is the base, 5 is the exponent
- 3.  $\left(\frac{3}{4}\right)\left(\frac{3}{4}\right)\left(\frac{3}{4}\right) = \left(\frac{3}{4}\right)^3$   $\frac{3}{4}$  is the base, 3 is the exponent

Note: The exponent only applies to what immediately precedes it.

4. Evaluate the following:

$$(-1)^5 = (-1) (-1) (-1) (-1) (-1) = -1$$
  
 $(-1)^8 = (-1) (-1) (-1) (-1) (-1) (-1) (-1) = 1$ 

These examples show that

- A power with a **negative base** has a **positive** value when the exponent is *even*.
- A power with a **negative base** has a **negative** value when the exponent is *odd*.

### **Square Root of a Number**

Finding the square root of a number is the opposite operation from squaring a number.

When you square a number, you multiply the number with itself.

Finding the square root means looking for a number that when multiplied with itself will form the larger number under the square root sign. When finding the square root, you can check your answer by squaring it (that is, by multiplying the number with itself) to see if you come back to the original number.

#### Example 1:

Squaring a number:  $5^2 = 5 \times 5 = 25$ 

Finding the square root of a number:  $\sqrt{25} = \sqrt{5 \times 5} = 5$ 

#### Example 2:

Squaring a number:  $9^2 = 9 \times 9 = 81$ 

Finding the square root of a number:  $\sqrt{81} = \sqrt{9 \times 9} = 9$ 

#### **Student practice:**



1. 
$$(-3)^3 =$$



2.  $\sqrt{100} =$ 



Scan the QR Code to the left, or use the link below: https://youtu.be/ROIfbUQrSY4

## Exercise 3.2

Solve the following numerical expressions.

1. 
$$8^2 =$$
 2.  $4^2 =$ 

3. 
$$(-5)^3 =$$
 4.  $(7)^2 =$ 

5. 
$$(-2)^5 = 6. \quad (-3)^3 =$$

7. 
$$(9)^2 = 8. \sqrt{36} =$$

9. 
$$\sqrt{64} = 10. \sqrt{144} =$$

11. 
$$\sqrt{9} = 12. \sqrt{49}$$

## **Division of Signed Numbers**

Students will make less sign mistakes if they think about signs first. If the signs are the same the answer is positive, if the signs are opposite the answer is negative. Then just divide the numbers

 $(-6) \div (-3) = (-) \div (-) = +$  then  $(6) \div (3) = 2$  answer is positive 2  $(+6) \div (-3) = (+) \div (-) = -$  then  $(6) \div (3) = 2$  answer is negative 2 Student see intro video <u>https://youtu.be/K\_tPbVPfHgk</u>

Division works the same as multiplication.

The quotient of two integers with *like* signs is positive.

$$(+8) \div (+2) = (+4)$$
  $(-8) \div (-2) = +4$ 

The quotient of two integers with *unlike* signs is negative.

$$(-8) \div (+2) = -4$$
  $(+8) \div (-2) = -4$ 

#### **Example:**

 $\frac{(+16)}{(-4)} = -4$  Remember, the fraction bar means **divide**.

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### **Summary of Division Rules**

- **Positive**  $\div$  **Positive** = **Positive**  $12 \div 3 = 4$
- Negative  $\div$  Negative = Positive  $(-12) \div (-3) = 4$
- Negative  $\div$  Positive = Negative  $(-12) \div 3 = -4$
- **Positive**  $\div$  **Negative** = **Negative**  $12 \div (-3) = -4$

#### **Student practice:**

- 1.  $8 \div (-2) =$
- 2.  $\frac{-16}{4} =$

#### 3. $-30 \div (-5) =$



Scan the QR Code to the left, or use the link below: https://youtu.be/bQ-KR3clFgs





### **Exercise 3.3**

Solve the following numerical expressions.

- 1.  $-1 \div (+1)$  2.  $-4 \div (-1) =$  

   3.  $(24) \div (4) =$  4.  $(-15) \div 5 =$  

   5.  $(-18) \div 3 =$  6.  $-6 \div (-2) =$  

   7.  $(-63) \div 9 =$  8.  $-12 \div (-3) =$
- 9.  $-12 \div (-4) =$  10.  $49 \div (-7) =$
- 11.  $-45 \div (-9) =$  12.  $72 \div (-8) =$
- 13.  $-10 \div (-2) =$  14.  $(18) \div (-6) =$
- 15.  $-56 \div (-7) =$  16.  $-1800 \div (-9) =$

## **Order of Operations with Integers**

Learners need to remember BEDMAS. Order of operations always stay the same. In the USA PEMDAS is used P represents parenthesis where in Canada B represents Brackets. Order of multiply and divide left to right are the same as well

Common errors are just working left to right and forgetting about BEDMAS

Students will see introductory video here https://youtu.be/ jiIOAV8Vr4

### Think about ...

- ♦ What is a numerical expression?
- ✦ Have you ever heard of BEDMAS?

### Keywords

Arithmetic operations	Addition, subtraction, multiplication, division, etc.
BEDMAS	An acronym used to help students remember in what order to perform operations: Brackets, Exponents, Division and Multiplication, Addition, and Subtraction
Numerical expression	A combination of numbers and one or more arithmetic operations; for example, $(4 + 5) \times 8 =$
Order of operations	The rules we follow when calculating numerical expressions

### **Order of Operations with Whole Numbers**

A numerical expression is a combination of numbers and one or more arithmetic operation symbols. Arithmetic operations are addition, subtraction, multiplication, and division.

The following are examples of numerical expressions:

- 4+20-7
- (2+3)-7
- $(6 \times 2) \div 20$
- $5 \div (20 \times 3)$

### **Order of Operations Rules**

BEDMAS is an acronym that stands for:

B	Brackets
E	Exponents
DM	<b>D</b> ivision and <b>M</b> ultiplication (left to right)
AS	Addition and Subtraction (left to right)

It is important to understand that

- Division and multiplication rank equally (and go left to right)
- Addition and subtraction rank equally (and go left to right)

#### Example 1:

2(5+9)-7 =	Brackets first 5+9 bring everything else down
2(14) - 7 =	Multiply next 2x14bring everything else dowm
28 - 7 = 21	Then subtract

#### Example 2:

 $(4+3) \times (6-3) \div 7 =$ 

According to BEDMAS, we perform operations in brackets first.

(4+3) = 7

Then we complete the brackets left to right.

(6-3) = 3

Next, we multiply.

 $7 \times 3 = 21$ 

And last, we divide.

 $21 \div 7 = 3$ 

So, using BEDMAS,

 $(4+3) \times (6-3) \div 7 = 3$  complete one step then bring everything else down 7  $\times$  3  $\div$  7 = 21  $\div$  7= 3

#### **Student practice:**

1. 
$$7 + 3 \times 5 =$$
 Instructor led Scan the QR Code to the left, or use the link below:

📋 Scan me

https://youtu.be/ClYdw4d4OmA Example 1 and 2

to the left,

2.  $(7+3) \times 4 \div 2 - 5 \times 6 =$ 

3.  $7 \times 2 + [7 + 3 \times (5 - 2)] - 4 \times 2 =$ 



Scan the QR Code to the left, or use the link below: https://youtu.be/pilcRV2dx7E

### **Exercise 3.4**

Solve the following numerical expressions. Remember, use the order of operations (BEDMAS).

- 1.  $5 + 3 \times 2 =$
- 2.  $12 6 \div 3 =$
- 3.  $(24-4) \div 5 =$
- 4.  $6 + (9 2)^2 =$
- 5.  $(22 18) \times (12 6) =$
- 6.  $(24+8) \div (14-10) =$
- 7.  $67 + (8 7) \times 3 + 5 =$
- 8.  $(34 14) + 16 \div 2(10 5) =$

9.  $67 - 2(17 + 8) - 10 + 2 \times 4 =$ 

10.  $(5 \times 7) + (12 - 6) =$ 

11. 17 + 12 - 8(12 - 9) =

12.  $(18 - 8) \times (20 - 10) =$ 

13.  $12 + (2 \times 8) - 18 \div 2 + 13 =$ 

14.  $64 \div (17 - 9) + 3(8 + 5) - 7 =$ 

## **Order of Operations with Integers and Exponents**

#### **Examples**

**Integers:** 

$-12 \div (8-5) - 10 =$	Brackets first
$-12 \div 3 - 10 =$	Division next
-4 - 10 = -14	Then add or subtract

#### **Exponents:**

$(-5)^2 - (4 - 7)^2 - 5 =$	Brackets first
$(-5)^2 - (-3)^2 - 5 =$	Exponents next
25 - 9 - 5 = 11	Then add or subtract

#### Absolute value brackets:

$(-5)^2 9-11  + (-3) =$	Brackets first
$(-5)^2 -2  + (-3) =$	Remember, the absolute value of $-2$ is $+2$
$(-5)^2 \times 2 + (-3) =$	Exponents next
$25 \times 2 + (-3) =$	Then multiply
50 + (-3) 47	Finally, add or subtract

#### **Student practice:**



1. 
$$-1[(-7) + 2(3 + 2)] - (5)^2$$



Scan the QR Code to the left, or use the link below: <u>https://youtu.be/gjrGd9TjjnY</u>

2. 
$$12 + (5 - 1) \times 3^2 - 8 \div \sqrt{4} =$$



### **Exercise 3.5**

Solve the following numerical expressions.

- 1.  $5-5^2 =$
- 2.  $2 (-5) + 3^2 =$
- 3.  $4(3^2) + 7(3+9) (-6) =$

4.  $6 \times \sqrt{25} - 4 \times \sqrt{16} =$ 

5.  $-17 + 8 \times \sqrt{9} - (11 - 5)^2 =$ 

6.  $|-12| \div 4 + 2 \times |(-2)^3| \div 4 =$ 

## **Problem Solving**

### **Tips for Solving Application Problems**

Read the tips below on solving application problems:

- **Step 1:** Read the question carefully. Read the problem several times.
- Step 2: Work out a plan. Write an equation to solve the problem.
- **Step 3:** Estimate. Is your answer reasonable?
- **Step 4:** Solve the problem. Is your answer reasonable?
- **Step 5:** Write a statement answering the problem.

#### Words that can be used to identify operations:

Addition	Subtraction	Multiplication	Division	Equals
sum	difference	product	quotient	is
total	minus	times	divide	is the same as
increased by	less than	double	per	equals
plus	more than	triple	divided equally	equal to
added to	decrease	of	divided by	results in
more	loss	twice		
gain	fewer			

### **Exercise 3.6**

Solve the following problems. Write your answers in sentence form.

- 1. A salesman takes a business trip and travels the following number of kilometres (km) each day: on Monday he travels 385 km, on Tuesday 412 km, on Wednesday 394 km, on Thursday 403 km, and on Friday 431 km. What is the total number of kilometres that he travelled that week?
- 2. Mary has volunteered to bake desserts for her school bake sale. She baked two dozen (24) cupcakes and plans to sell them for \$3.25 each. She also baked a dozen (12) brownies and will sell them for \$2.50 each. How much money will Mary raise if she sells all of her baked goods?
- 3. In June, the Anderson family made four deposits of \$1 782 each to their bank account. They also withdrew \$5 931 for expenses. What was their account balance for the month of June, assuming they had no money in the account at the start of the month?
- 4. A group of six students is planning a summer trip to Germany. The total cost of all six flights is \$8 400. Each person will pay \$600 for hotel fees. If the six students all pay equally for the flights, what is the cost of the entire trip for each student, including the hotel fees?
- 5. On Sunday, June 21, the temperature was 27°C. The temperature dropped 2°C per day over the next seven days. What was the temperature on June 28?

## **Unit 4: Operations with Signed Decimals**

Introductory Video to Operations with signed decimals



## Adding and Subtracting Signed Decimals

## **Adding Signed Decimals**

If the signs are the same, add the numbers and the sign remains the same.

#### **Example 1:** -9.087 + -15.31

9.087	Step 1: Line up the decimals and add zeros if necessary
+ 15.310	Step 2: The signs are the same (both negative), so add the decimals and keep
-24.397	the negative sign. Since both signs are negative, the answer is
	negative.

If the signs are opposite, use the absolute value of each number. Then subtract the smaller absolute value from the larger absolute number. The sign of the larger number will be the sign of your answer.

#### **Example 2:** (+9.087) + (-15.31)

15.310	Step 1: Line up the decimals again, putting the largest absolute value on top.
- 9.087	15 is larger than 9, so it needs to go first.
-6.223	<b>Step 2:</b> Subtract the numbers. Since the larger number $(-15.31)$ is negative,
	the answer is also negative.

### **Subtracting Signed Decimals**

When subtracting signed decimals, change the subtraction sign to addition, and change the sign of the number behind it to its opposite. Then follow the rules for adding signed decimals.

**Example:** (-12.2) – (-15.31)

(-12.2) + (+15.31)	<b>Step 1:</b> Change the subtraction sign to addition and change the sign of the number behind it to its opposite
15.91	Step 2: Since the signs are opposite, subtract the absolute values. The
-12.20	largest number is positive, so the answer will be positive.
+3.71	

### **Exercise 4.1**

Solve the following numerical expressions.

- 1. (24.008) + (-0.995) = 2. (-6.05) + (-39.7) =
- 3. 0.9 7.29 = 4. (-2) 4.99 =
- 5. -5.009 + 0.73 = 6. -1.7035 (-6.7) =
- 7. 8000 + (-8002.63) 8 = 8. -6.5 + 0.7 =
- 9. -42.671 194.9 = 10. -8.4 + (-50.83) =
- 11. 0.77 3.06 = 12. -6.409 + 8.224 =
- 13. -489.7 38 = 14. (+11.3) (-25.652) (+13.91) =
- 15. 12.2 (+15.2) + (-34.7) (-12.8) = 16. (-1.3) (+0.5) (-3.8) (-9.7) =

## **Multiplying and Dividing Signed Decimals**

## **Multiplication Rules of Signs**

- **Positive** × **Positive** = **Positive**
- Negative × Negative = Positive
- Negative × Positive = Negative
- **Positive** × Negative = Negative
- Brackets together means to multiply

#### **Example:** -0.008 × 0.06

-0.008 Apply the rule **Negative** × **Positive** = **Negative** 

 $\times 0.06$  Multiply as normal and add the negative sign to the result.

-0.00048

## **Division Rules of Signs**

- **Positive** ÷ **Positive** = **Positive**
- Negative ÷ Negative = Positive
- Negative ÷ Positive = Negative
- Positive ÷ Negative = Negative

#### **Example:** 0.3 - 0.0036

3)-0.036Move the decimal in the first number once to the right and do the same for<br/>the second number.-0.006Apply the rule Negative  $\div$  Positive = Negative and put a negative sign in the<br/>answer.3)-0.036answer.36Now divide as normal.



## Exercise 4.2

Solve the following numerical expressions.

1.  $(-0.72) \times (-0.06) =$  2.  $2.3 \times (-0.8) =$ 

3. (-0.1)(-3.5) = 4.  $(-0.6) \times 0.3 =$ 

5.  $0.42(-1.9) = 6. (-0.6) \times (-0.8) =$ 

7. (-1.2)(6.8) = 8. (-4.37)(-2.08) =

9.  $27.3 \div (-7) =$  10.  $-4.23 \div -9 =$ 

11.  $(-20.01) \div (-0.5) =$  12.  $54 \div -1.5 =$ 

13. 
$$(-0.108) \div 1.8 =$$
 14.  $-3.1 \div -0.006 =$ 

15.  $(-1.7) \div 0.09 =$  16.  $-240.8 \div 9 =$ 

17.  $(-27.3) \div 100 =$  18.  $(-2) \div (-20) =$ 

## **Order of Operations with Decimals**

Order of operations is the same as order of operations with whole numbers. Learners need to remember BEDMAS. Common errors are just working left to right

#### **Example:**

-0.75 + 0.8(-0.6 + 0.2) = Brackets first-0.75 + 0.8(-0.4) = Multiply next0.75 - 0.32 = -1.07 Then add or subtract

### Student practice:

$$12 - [0.3 - (2.8 - 0.1^2)] =$$



### **Exercise 4.3**

Find the solutions to the following numerical expressions. Remember to use the order of operations rules (BEDMAS).

- 1.  $-8.9 + 4^2 \div (-0.02) =$
- 2. (-0.18 + 2.5) + 4(0.05) =
- 3.  $-0.7(-3) (-0.04) \div 2 =$
- 4. Gino had –\$15.46 in his bank account at the end of June. During the month of July, he made deposits of \$75.38 and \$182.25. He made two withdrawals of \$98.99 and \$159.26. How much money is in his bank account at the end of July?

## **Unit 5: Operations with Signed Fractions**

The rules don't change for operations with fractions. All that changes for signed fractions is how the signs are affected. The same rules apply as for integers.

## Adding and Subtracting Signed Fractions

## **Adding Signed Fractions**

If the signs are the same, add the fractions and the sign remains the same.

• Remember to find the lowest common denominator first, if necessary.

#### Example 1:

$-\frac{3}{4} + \left(-\frac{5}{6}\right) =$	<b>Step 1:</b> Find the lowest common denominator. For 4 and 6, it is 12.
$-\frac{3\times3}{4\times3} + \left(-\frac{5}{6}\right) \frac{\times2}{\times2} =$	<b>Step 2:</b> Multiply the numerator and denominator by the same number to make both denominators 12.
$-\frac{9}{12} + \left(-\frac{10}{12}\right) = -\frac{19}{12}$	<b>Step 3:</b> Rewrite the fractions with the common denominator and add the numerators.
$= -1\frac{7}{12}$	<b>Step 4:</b> Change the fraction to a mixed number.

If the signs are opposite, use the absolute values of the numbers. Subtract the smaller absolute value from the larger absolute value. The sign of the larger number will be the sign of your answer.

#### Example 2:

- $\frac{5}{12} + \left(-\frac{5}{9}\right) =$  To find the common denominator, use the product of prime factors:
  - 12 is  $(\mathbf{2} \times \mathbf{2} \times 3)$  and 9 is  $(\mathbf{3} \times \mathbf{3})$
  - The common denominator is  $(2 \times 2) \times (3 \times 3) = 36$

 $\frac{15}{36} + \left(-\frac{20}{36}\right) = \left(-\frac{5}{36}\right)$  The signs are opposite, so subtract the absolute values: 20 - 15 = 5

The largest number is negative, so the answer will be negative.

### **Subtracting Signed Fractions**

#### **Example:**

When subtracting signed fractions, change the minus sign to addition and change the sign of the number behind it to its opposite. Then follow the rules for adding signed fractions.

$$-2\frac{1}{2} - \left(+3\frac{3}{4}\right) =$$

Find a common denominator and change subtraction to addition.

 $-2\frac{2}{4} + \left(-3\frac{3}{4}\right) = -5\frac{5}{4}$ 

The signs are the same (both negative), so the answer will be negative. Add the whole numbers, then add the fractions.

=-  $-6\frac{1}{4}$  Finally, reduce to lowest terms.

#### **Student practice:**



1. 
$$-\frac{3}{4} - \frac{7}{6} - \frac{3}{6} =$$



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2.  $3\frac{1}{8} + \frac{3}{4} + \left(-2\frac{1}{6}\right) =$ 



### Exercise 5.1

Solve the following numerical expressions.

1.  $\left(-\frac{1}{14}\right) + \left(-\frac{3}{7}\right) =$ 2.  $\left(-\frac{2}{9}\right) + \frac{2}{3} =$ 3.  $\frac{3}{4} + \frac{1}{8} =$ 4.  $\left(-\frac{5}{8}\right) - \left(-\frac{1}{12}\right) =$ 

5. 
$$-\frac{7}{24} - \frac{3}{8} =$$
 6.  $-2 + \frac{3}{5} =$ 

7. 
$$\left(-\frac{7}{9}\right) - \frac{5}{6} = 8. \left(-\frac{7}{9}\right) - \left(-\frac{3}{6}\right) =$$

9. 
$$\left(+\frac{8}{20}\right) - \left(+\frac{4}{5}\right) = 10. \left(-\frac{3}{4}\right) + \frac{5}{8} =$$

11. 
$$-2\frac{1}{2} + \left(-3\frac{4}{5}\right) =$$
 12.  $5\frac{1}{3} - 8\frac{1}{4} =$ 

13. 
$$-16\frac{3}{7} + \left(-27\frac{2}{3}\right) =$$
 14.  $12\frac{5}{8} + \left(-15\frac{2}{7}\right) =$ 

15. 
$$-6\frac{1}{2} + 3\frac{2}{3} + \left(-7\frac{5}{6}\right) =$$
 16.  $-6\frac{1}{5} - 3\frac{2}{5} - 4\frac{9}{10} =$ 

17. 
$$-3\frac{1}{3} - 15\frac{5}{9} - 13\frac{11}{18} =$$
 18.  $17\frac{1}{8} + 13\frac{2}{3} + \left(-22\frac{5}{6}\right) =$ 

19. 
$$\frac{1}{3} + \left(-\frac{3}{5}\right) + \frac{7}{15} - \frac{5}{30} + \left(-\frac{7}{10}\right) =$$

20. 
$$2\frac{1}{2} + \left(-4\frac{9}{16}\right) + 8\frac{1}{4} - 7\frac{5}{8} =$$

## **Multiplying and Dividing Signed Fractions**

## **Multiplying Signed Fractions**

### **Multiplying Rules of Signs**

- **Positive** × **Positive** = **Positive**
- Negative × Negative = Positive
- Negative × Positive = Negative
- **Positive** × **Negative** = **Negative**
- Brackets together means to multiply

### Remember the steps for multiplying fractions:

- Step 1: Change whole numbers or mixed numbers to improper fractions.
- Step 2: Reduce any number from the numerator with any number from the denominator.
- Step 3: Multiply the numerators, then multiply the denominators.
- Step 4: Change an improper fraction to a mixed fraction or whole number.

#### Example:

$$3 \times \left(-\frac{2}{3}\right) = \frac{3}{1} \times \left(-\frac{2}{3}\right)$$
$$= \frac{3^{1}}{1} \times \left(-\frac{2}{3}\right)$$
$$= -\frac{2}{1} = -2$$

#### Student practice:

1. 
$$-7 \times \frac{3}{49} =$$

2.  $-\frac{5}{9} \times \left(-\frac{3}{15}\right) =$ 

Instructor led



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### **Dividing Signed Fractions**

#### **Division Rules of Signs**

- **Positive** ÷ **Positive** = **Positive**
- Negative ÷ Negative = Positive
- Negative ÷ Positive = Negative
- **Positive** ÷ Negative = Negative

#### Remember the steps for dividing fractions:

- Step 1: Change whole numbers or mixed numbers to improper fractions.
- Step 2: Never divide—always multiply by the reciprocal.
- Step 3: Reduce any number from the numerator with any number from the denominator.
- Step 4: Multiply the numerators, then multiply the denominators.
- Step 5: Change an improper fraction to a mixed fraction or whole number.

#### **Example:**

$$3 \div \frac{2}{3} = -\frac{3}{1} \div \frac{2}{3}$$
$$= -\frac{3}{1} \times \frac{3}{2}$$
$$= -\frac{3 \times 3}{1 \times 2} = -\frac{9}{2} = -4\frac{1}{2}$$

**Student practice:** 





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 $2. \quad -4 \div \left(-\frac{1}{2}\right) =$ 

## Exercise 5.2

Solve the following numerical expressions.

1. 
$$-\frac{3}{8} \times \left(-\frac{12}{5}\right) =$$
 2.  $\frac{2}{3} \times \left(-\frac{6}{7}\right) =$ 

3. 
$$-\frac{4}{9} \times \frac{3}{8} =$$
 4.  $\left(-\frac{21}{30}\right) \left(\frac{5}{7}\right) =$ 

5. 
$$\left(-\frac{6}{11}\right)\left(-\frac{22}{15}\right) = 6. -\frac{9}{14} \times \left(-\frac{49}{72}\right) =$$

7. 
$$10 \times \left(-\frac{3}{5}\right) =$$
 8.  $-27 \times \left(-\frac{3}{15}\right) =$ 

9. 
$$-20 \times \frac{4}{5} =$$
 10.  $21 \times \left(-1\frac{5}{7}\right) =$ 

11. 
$$\frac{4}{3} \div \left(-\frac{8}{9}\right) =$$
 12.  $-\frac{8}{15} \div \left(-\frac{4}{25}\right) =$ 

13. 
$$\frac{5}{9} \div \left(-\frac{10}{27}\right) =$$
 14.  $-\frac{7}{10} \div 14 =$ 

15. 
$$-\frac{5}{6} \div (-10) =$$
 16.  $4\frac{1}{2} \div (-18) =$ 

17. 
$$-\frac{9}{16} \div \frac{18}{24} \div \left(-\frac{1}{2}\right) =$$
 18.  $-5 \div \left(-3\frac{1}{3}\right) =$ 

$$19. \ \left(\frac{4}{11}\right)\left(-\frac{22}{25}\right)\left(\frac{20}{11}\right)\left(\frac{5}{6}\right)\left(-\frac{9}{8}\right) = 20. \ -\frac{2}{3}\times\left(-\frac{6}{14}\right)\times\frac{21}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{2}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{2}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{2}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{1}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{1}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{1}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{1}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{8}{9} = 20. \ -\frac{1}{3}\times\left(-\frac{6}{14}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\left(-\frac{3}{4}\right)\times\frac{1}{24}\times\left(-\frac{3}{4}\right)\times\left(-\frac{3}{4$$

## **Order of Operations with Fractions**

Order of operations is the same as order of operations with whole numbers. Learners need to remember BEDMAS. Common errors are just working left to right

#### Examples

**Fraction bar:** 

$\frac{-5+3^2}{16-7(2)} =$	Step 1:	Simplify the numerator. $-5 + 3^2 = -5 + 9 = 4$
	Step 2:	Simplify the denominator. 16 - 7(2) = 16 - 14 = 2
$\frac{-5+3^2}{16-7(2)} = \frac{4}{2} = 2$	Step 3:	Simplify the fraction.

**Fractions:** 

$-\frac{3}{4} + \left(-\frac{1}{2}\right)^2 \div \frac{2}{3} =$	Step 1: Do the exponents first.
$-\frac{3}{4} + \frac{1}{4} \div \frac{2}{3} =$	<b>Step 2:</b> Divide (remember that with fractions, you multiply by the reciprocal)
$-\frac{3}{4} + \frac{1}{4} \times \frac{3}{2} =$	
$-\frac{3}{4} + \frac{3}{8} =$	Step 3: Find the lowest common denominator.
$-\frac{6}{8} + \frac{3}{8} = -\frac{3}{8}$	Step 4: Add or subtract and simplify if necessary.

#### **Student practice:**

1. 
$$\frac{3(6-8\div4)}{5\times2-3^2} =$$

Instructor led



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2. 
$$\left(\frac{2}{3}\right)^2 - \frac{5}{6} \times \frac{1}{2} + \frac{3}{4} \div \frac{1}{3} =$$



## Exercise 5.3

Solve the following numerical expressions.

1. 
$$\frac{-6+3^2-(-7)}{7-9-3} =$$

2. 
$$\frac{-9+18 \div (-3)(-6)}{32-4(12) \div 3(2)+3} =$$

3. 
$$\frac{3}{5}\left(\frac{1}{3}\right) + \frac{2}{5}\left(\frac{3}{4}\right) =$$

$$4. \quad \left(\frac{7}{8} - \frac{3}{4}\right) \div \frac{3}{2} =$$

5. 
$$\frac{3}{8}\left(\frac{1}{4} + \frac{1}{2}\right) \times \frac{32}{3} =$$

6. 
$$\left(\frac{1}{3} + \frac{1}{6}\right)^2 - 3\left(\frac{2}{3} - \frac{1}{9}\right) =$$

7. 
$$9\left(\frac{1}{3}\right)^3 \times \left(\frac{4}{3}\right)^2 =$$

8. 
$$\left(\frac{5}{6} - \frac{7}{12}\right) - \frac{3}{4}\left(\frac{1}{3}\right)^2 =$$

9. 
$$\left(\frac{2}{3}\right)^2 - \left(\frac{5}{8} - \frac{1}{2}\right) \div \frac{3}{2} =$$

## **Post-Module Assessment and Glossary**

## **Post-Module Assessment**

Now that you have completed this module, reassess what you can do against this checklist:

	In this module, I will learn how to	I can't do this	I can do this with help	I can do this!
1.	Solve numerical expressions with negative and positive numbers			
2.	Solve numerical expressions using the order of operations			

## **Glossary for this Module**

Arithmetic operations	Addition, subtraction, multiplication, division, etc.
Base	The number the exponent is attached to; in the power $4^2$ , the base is <b>4</b>
BEDMAS	An acronym used to help students remember in what order to perform operations: Brackets, Exponents, Division and Multiplication, Addition and Subtraction
Exponent	The number attached to the base that tells you how many times the base is multiplied with itself; in the power $4^2$ , the exponent is <b>2</b>
Integer	A number that is written without a fractional component; it can positive or negative
Like signs	Signs that are the same
Negative whole numbers	Numbers less than zero, such as $-1, -2, -3 \dots$
Numerical expression	A combination of numbers and one or more arithmetic operations; for example, $(4 + 5) \times 8 =$
Order of operations	The rules we follow when calculating numerical expressions
Positive whole numbers	Numbers greater than zero, such as 1, 2, 3,

Power	The base and exponent together; for example, $4^2$ is a power and means $4 \times 4$
Product	The answer when two or more numbers are multiplied together
Quotient	The answer when one number is divided by another
Square root	The opposite of squaring a number. The number in the square root sign, or <i>radical</i> , is a product of a number multiplied with itself; for example $\sqrt{16} = \sqrt{4 \times 4} = 4$ 4 is the result of $\sqrt{16}$ , which means that <b>4 is the square root of 16</b>
Subtracting integers	Add the opposite of the second sign
Unlike signs	Signs that are opposite

## **Appendix: Exercise Answer Key**

## **Unit 1: Introduction to Signed Numbers**

## Exercise 1.1

1.	-\$5	500	2.	300, +3	300 3.		-7	4.	3,	+3	5.	-20%
6.	-7		7.	\$50, +\$	\$50 8.		-30	9.	7(	000, +7000	10	). –12
Ex	er	cise 1.2										
1.	a.	-4 should	be c	ircled			b.	3 shou	ld b	e circled		
	c.	5 should b	e cii	cled			d.	0 shou	ld b	e circled		
	e.	-1 should	be c	ircled								
2.	a.	<	1	o. >	C	2.	<		d.	<	e.	<
	f.	>	į	g. <	ł	1.	>		i.	<	j.	>
3.	a.	8	1	o. 0	C	2.	15		d.	37	e.	218
	f.	45										

## **Unit 2: Addition and Subtraction of Integers**

### Exercise 2.1

619 7. 100 8. 10 9122	10. –403											
1110 12. 13 1311 14. 5	15. –41											
167 1719 18. 6 19. 15	20. –39											
Exercise 2.2												
13 22 317 44 5	-3 63											
714 8. 32 9. 0 10. 58 11	-43 1242											
1337 14. 23 1549 16. 21												

### **Exercise 2.3**

- 1. The change in temperature was 8°C.
- 2. No, they did not gain enough yards to keep the ball.
- 3. Jim has \$28 left in his bank account.
- 4. The temperature the next day was  $4^{\circ}$ C.
- 5. The temperature at 7 p.m. was –25 degrees C.

## Unit 3: Multiplication and Division of Signed Numbers

#### **Exercise 3.1**

1.	-10		2. –48	3		3.	-1	6		4.	-14		5.	7	
6.	-18		7. –63	\$		8.	-4	8		9.	-49		10	. 56	5
11.	-24		12. –56	50		13.	64			14	. –54		15	. –2	210
16.	400		17. 56			18.	-2-	40		19	0. –320		20	. 54	0
Ex	ercise	3.	2												
1.	64	2.	16		3.	-125		4.	49		5.	-32		6.	-27
7.	81	8.	6		9.	8		10.	12		11.	3		12.	5
Ex	ercise	3.	3												
1.	-1	2.	4		3.	6		4.	-3		5.	-6		6.	3
7.	-7	8.	4		9.	3		10.	-7		11.	5		12.	-9
13.	5	14	4. –3		15.	8		16.	200						
Ex	ercise	3.	4												
1.	11	2.	10	3.	4		4.	55	5	5.	24	6.	8	7.	. 75
8.	60	9.	15	10.	41		11.	5	1	2.	100	13.	32	14	4. 40

### **Exercise 3.5**

1. -20 2. 16 3. 126 4. 14 5. -29 6. 7

### **Exercise 3.6**

- 1. The salesman travelled 2 205 km during the week.
- 2. Mary will raise \$108.
- 3. Their account balance was \$1 197.
- 4. The cost for each student would be \$2 000.
- 5. The temperature was 13°C on June 28.

## **Unit 4: Operations with Signed Decimals**

### **Exercise 4.1**

1. 23.013	245.75	36.39	46.99	54.279	6. 4.9965
710.63	8. –5.8	9. –237.571	1059.23	11. –2.29	12. 1.815
13527.7	14. 23.042	15. –24.9	16. 11.7		

### **Exercise 4.2**

1.	0.0432	21.	84 3.	0.35	4.	-0.18	5.	-0.798	6.	0.48
7.	-8.16	8. 9.0	896 9.	-3.9	10.	0.47	11.	40.02	12.	-36
13.	-0.06	14. 516	5.667 15.	-18.889	16.	-26.756	17.	-0.273	18.	0.1

#### **Exercise 4.3**

1808.9 2. 2.52 3. 2.12 4. There is -\$16.08 in hi	s bank account
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## **Unit 5: Operations with Signed Fractions**

## Exercise 5.1

1.	$-\frac{1}{2}$	2. $\frac{4}{9}$	3. $\frac{7}{8}$	4. $-\frac{13}{24}$	5.	$-\frac{2}{3}$
6.	$-1\frac{2}{5}$	7. $-1\frac{11}{18}$	8. $-\frac{5}{18}$	9. $-\frac{2}{5}$	10.	$-\frac{1}{8}$
11.	$-6\frac{3}{10}$	12. $-2\frac{11}{12}$	13. $-44\frac{2}{21}$	14. $-2\frac{37}{56}$	15.	$-10\frac{2}{3}$
16.	$-14\frac{1}{2}$	17. $-32\frac{1}{2}$	18. $7\frac{23}{24}$	19. $-\frac{2}{3}$	20.	$-1\frac{7}{16}$
Ex	ercise 5.	2				
1.	$\frac{9}{10}$	2. $-\frac{4}{7}$	3. $-\frac{1}{6}$	4. $-\frac{1}{2}$	5.	$\frac{4}{5}$
6.	$\frac{7}{16}$	7. –6	8. $5\frac{2}{5}$	9. –16	10.	-36
11.	$-1\frac{1}{2}$	12. $3\frac{1}{3}$	13. $-1\frac{1}{2}$	14. $-\frac{1}{20}$	15.	$\frac{1}{12}$
16.	$-\frac{1}{4}$	17. $1\frac{1}{2}$	18. $1\frac{1}{2}$	19. $\frac{6}{11}$	20.	$-\frac{1}{6}$
Ex	ercise 5.	3				
1.	-2	2. 9	3. $\frac{1}{2}$	4. $\frac{1}{12}$	5.	3
6.	$-1\frac{5}{12}$	7. $\frac{16}{27}$	8. $\frac{1}{6}$	9. $\frac{13}{36}$		