Foundational Numeracy

Module 7: Ratios, Rates, and Percent

Solutions Manual

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Developed for Alberta's Community Adult Learning Program



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Introduction to the Module

In this module, you will learn to solve problems using proportions and percent in ways that can be applied to everyday problems. In the process, you will develop an understanding of ratios and rates, proportions, and percent. Enjoy your studies!

Important

When you see an object like the one below, you can use a QR code scanner on your phone or tablet, and it will play a video of the math example.



Specific Learning Outcomes

The table below displays the skills and knowledge you will explore in this module. This is your opportunity to evaluate your own skills to see if you can do these things. At the end of this module, you will be invited to re-evaluate your skills to measure the progress you have made.

	In this module, I will learn how to	I can't do this	I can do this with help	I can do this!
1.	Work with ratios and rates			
2.	Solve proportions			
3.	Work with percent			
4.	Change between fractions, decimals, and percents			
5.	Solve application problems with proportions and percents			

Essential Skills

The following essential skills are used in this module:



Reading: Understanding materials written in sentences or paragraphs



Numeracy: Using and understanding numbers



Computer use/digital technology: Using computers and other tools such as calculators and phones



Vocabulary: Gaining related vocabulary



Thinking: Finding information, problem solving, decision making, using your memory, planning job tasks and being organized, critical thinking

Module 4: Keywords

Ratio	A comparison of two quantities by division	
Rate	The comparison by division of two quantities that are measured in different units	
Equivalent	Equal	
Proportion	Two or more equivalent ratios	
Percent	A ratio that is always given out of 100	
Solving proportions	Solving for an unknown value	

Unit 1: Ratios and Rates

Ratios

Think about ...

Imagine that a class contains 27 students. There are 12 male students and 15 female students.

With this information, you can make several numerical comparisons about the students in the class. Such a comparison is called a **ratio**. The order of the numbers is very important.

A ratio is a comparison of one number with another.

- It is used to show the relationship between the number of one thing and the number of another thing.
- ✤ When you write a ratio, you must keep in mind which number belongs to which thing.
- + The order of the numbers in a ratio is important.

Example 1

How many males are there compared to females? There are 12 males compared to 15 females. This ratio can be written in the three ways.

• This ratio is written as 12 to 15, or 12:15, or $\frac{12}{15}$.

Since males come first in the question, males come first in the ratio.

It is important to reduce ratios to lowest terms.

★ $\frac{12}{15} = \frac{4}{5}$ Therefore, for every 4 males in the class, there are 5 females.

You could also think about this ratio in another way: "How many females are there compared to males?"

- There are 15 females compared to 12 males, so the ratio is 15 to 12, or 15:12, or $\frac{15}{12}$.
- Next, reduce the ratio to lowest terms: $\frac{15}{12} = \frac{5}{4}$

This ratio means that there are 5 females in the class for every 4 males. In this case, the fraction is improper.

Note: When working with ratios, we never convert improper fractions to mixed numbers or whole numbers as the ratio would lose its meaning.

We could also use the information above to compare the number of males to the total number of students in the class or the number of females to the total number of students.

- ★ The comparison of the number of males to all the students in the class is written numerically as 12:27 or $\frac{12}{27}$. This would be read as "12 to 27" or "12 out of 27."
- Next, reduce the ratio to lowest terms: $\frac{12}{27} = \frac{4}{9}$

This ratio means that 4 out of every 9 students are males.

Remember: When ratios are written as fractions, they are usually reduced to their lowest terms, even improper fractions, but you should not change an improper fraction to a whole number or a mixed number.

Example 2

Write a ratio comparing 2 minutes to 60 seconds.

In this example, it is important to convert so that both times use the same unit of measurement.

♦ 60 seconds is equal to 1 minute.

Or

✤ 2 minutes is equal to 120 seconds.

Both conversions are correct.

1. If you use seconds as the unit of measurement:

120 to
$$60 = \frac{120}{60} \div \frac{60}{60} = \frac{2}{1}$$

2 minutes to 60 seconds is a ratio of 2 to 1.

2. If you use minutes as the unit of measurement:

2 to
$$1 = \frac{2}{1}$$

Student practice:

- 1. There are 10 horses and 5 dogs.
 - a. Write a ratio comparing horses to dogs.
 - b. Write a ratio comparing dogs to horses.
- 2. Compare 5 dimes to 4 nickels.



Exercise 1.1

- 1. Write the following comparisons as ratios reduced to the lowest terms.
 - a. A recipe calls for 3 cups of flour and 1 cup of milk. Write the ratio of flour to milk.

$$\frac{3}{1}$$
 or 3 °l

b. There are 16 green marbles and 4 blue marbles in a bag. Write the ratio of blue marbles to the total number of marbles.

$$16+4=20 \text{ marbles}, \frac{4}{20} = \frac{1}{5} \text{ or } 1.5$$

c. The police checked 75 vehicles. They found that 15 vehicles did not meet the safety standards, but 60 of them did. Write a ratio comparing the unsafe vehicles to the safe vehicles. 15151

d. The police checked 120 vehicles. They found that 30 vehicles did not meet the safety standards, but 90 of them did. Write a ratio comparing the unsafe vehicles to the total number of vehicles.

e. At a barbeque, 36 hotdogs and 18 hamburgers were eaten. Write the ratio of hotdogs eaten to hamburgers eaten.

$$\frac{36 \div 18}{18 \div 18} = \frac{2}{1} \quad \text{or} \quad 20$$



2. Write each of the following as ratios in two ways. Reduce the ratios to lowest terms.

a. The value of 16 dimes to the value of 20 pennies
16 dimes = 160 pennies
$$\frac{160 \div 20}{20 \div 20} = \frac{8}{1}$$
 or $\frac{20 \text{ pennies}}{\frac{16}{20} \div 20} = \frac{8}{1}$
b. The value of 12 dimes to the value of 36 nickels
12 dimes = 24 nickels $\frac{24 \div 12}{36 \div 12} = \frac{2}{3}$ or $\frac{36}{2} = \frac{1}{1}$
c. 15 dogs to 45 cats $\frac{15}{36} \div 12 = \frac{2}{3}$ or $\frac{12}{36} \div \frac{2}{18} = \frac{2}{3}$
d. 0.18 metres to 0.12 metres
 $\frac{0.18 \times 100}{0.12 \times 100} \div \frac{18}{12} = \frac{3}{2}$ or $3^{\circ}_{0}_{0}_{0}_{0}_{0}$
e. 20 minutes to 3 hours
 $3howrs = 180$ minutes $\frac{20}{180 \div 20} = \frac{1}{9}$ or $1^{\circ}_{0}_{0}_{0}$

Rates

Think about ...

- ✤ Speed in kilometres per hour
- ✦ Fuel consumption in kilometres per litre
- ♦ Wages in dollars per hour
- ✤ Cost in dollars per kilogram

These are all examples of rates. Rates may be expressed as ratios in reduced form. Note that in each example below, the rate is expressed as a simplified ratio with the second term equal to 1.

Examples

Ra	te	Ratio
1.	50 kilometres (km) per hour (hr)	50 km/1 hr or 50 km:1 hr
2.	80 kilometres in 2 hours	80 km/2 hr = 40 km/1 hr or 40 km:1 hr
3.	90 cents for 6 grams (g)	$90\phi/6 \text{ g} = 15\phi/1 \text{ g or } 15\phi:1 \text{ g}$
4.	\$12 for 3 people	\$12/3 people = \$4/1 person or \$4:1 person

Note: Because the units are different for each part of the rate, they will not cancel and must be kept.

Student practice:

Jayda takes 3 hours to deliver 189 newspapers on her route. What is her rate per hour at which she delivers her papers?



Exercise 1.2

Express each of the following rates as a ratio in simplest form with the second term equal to 1. Be sure to keep your units.

1. 95 cents a dozen

- 2. 100 kilometres per hour 100 km/1 hour or 100 km/hour 100 km/
- 3. 18 metres for \$9 $\frac{18 \text{ m}}{\$9} = \frac{2 \text{ m}}{\$_1}$
- 4. 18 kilometres per litre $\frac{18 \text{ km}}{1 \text{ L}} \quad \text{or} \quad 18 \text{ km}/\text{L}$ 5. 52 cars per minute $\frac{52 \text{ cars per minute}}{52 \text{ cars}} \quad 52 \text{ cars}/\text{min}$

6. 3 000 revolutions in 2 minutes

8. 20 tablespoons for each 5 kilograms

7.

9. 80 cents for 10 grams

9. 80 cents for 10 grams

$$\frac{80^{k}}{10g} = \frac{8^{k}}{1g} \text{ or } 8^{k}/9$$
10. \$3.60 for 3 light bulbs

$$\frac{\$ 3.60}{3 bulbs} = \frac{\$ 1.20}{1 bulb} \text{ or } \$ 1.30/bulb$$
11. 1 000 kilometres in 4 hours

$$\frac{1000 \text{ Km}}{4 \text{ hrs}} = \frac{250 \text{ Km}}{1 \text{ hr}} \text{ or } 250 \text{ Km}/\text{hr}$$
12. 50 homes have 275 clocks

$$\frac{275 \text{ clocks}}{5^{\circ}0 \text{ homes}} = \frac{5.5 \text{ clocks}}{1 \text{ home}} \text{ or } 5.5 \text{ clocks}/\text{home}$$
13. 732 beats in 10 minutes

$$\frac{732 \text{ beat + s}}{1000 \text{ min}} = \frac{73.2 \text{ beat } \text{s}}{1 \text{ min}} \text{ or } 73.2 \text{ beat } \text{s}/\text{min}$$
14. 450 kilometres on 25 litres of fuel

$$\frac{450 \text{ Km}}{254} = \frac{18 \text{ Km}}{1 \text{ L}} \text{ or } 18 \text{ Km}/\text{L}$$

15. A ratio of distance travelled to time is called speed. If you travel 45 kilometres in 3 hours, what is your rate (speed) in kilometres per hour (km/h)?

Unit 2: Proportions

Proportions (Equivalent Ratios)

A proportion is a mathematical statement that two ratios are equal.

This is how a proportion is shown: $\frac{15}{10} = \frac{3}{2}$ or 15:10 = 3:2

✤ It is read: "Fifteen is to ten as three is to two."

For example, we know that 6 eggs out of a container of 12 eggs is the same as $\frac{1}{2}$ a dozen eggs. By equating the ratios, $\frac{6}{12} = \frac{1}{2}$, we form a proportion.

Method 1: Use Equivalent Fractions by Reducing to Lowest Terms

Make equivalent fractions to determine whether a proportion is true.

If a proportion is true, the fractions are equivalent.

 $\frac{6}{12} = \frac{1}{2}$ $\frac{6 \div 6}{12 \div 6} = \frac{1}{2}$ These are equivalent fractions.

Example 1

Is the proportion true?

 $\frac{3}{5} = \frac{6}{10}$

Reduce $\frac{6}{10}$ to lowest terms:

 $\frac{6 \div 2}{10 \div 2} = \frac{3}{5}$ The fractions are equivalent.

Thus, $\frac{3}{5}$ and $\frac{6}{10}$ form a true proportion.

Example 2

Is the proportion true?

$$\frac{6}{8} = \frac{18}{21}$$

Reduce each fraction to lowest terms:

$$\frac{6}{8} = \frac{3}{4}$$
 and $\frac{18}{21} = \frac{6}{7}$

 $\frac{3}{4} \neq \frac{6}{7}$ Since these two ratios are not equal, we would say the proportion is false.

Method 2: Use Cross-Multiplication or Cross Products

Example 1

 $\frac{2}{5}$ $\frac{4}{10}$ $2 \times 10 = 20$ $5 \times 4 = 20$

Since the cross products are equal, the proportion is true. So $\frac{2}{5} = \frac{4}{10}$.

Example 2

 $3 \times 10 = 30$ $5 \times 7 = 35$

Since the cross products are not equal, the proportion is false. So $\frac{3}{5} \neq \frac{7}{10}$.

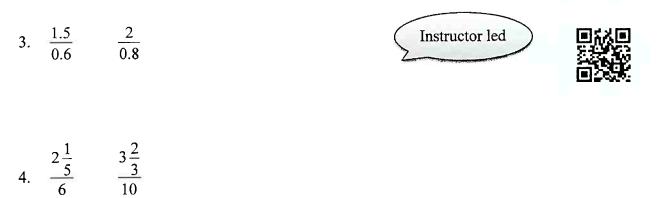
Student practice:

1. $\frac{12}{15}$ $\frac{16}{20}$ Instructor led	\supset
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2. 7:9 30:45

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Exercise 2.1

Use either method to determine whether each proportion is true or false. If the proportion is true, write = between the ratios. If the proportion is false, write \neq between the ratios (\neq means *not* equal).

Using reducing to lowest terms	Using Cross Products
1. $\frac{4}{8} = \frac{5}{10}$ $\frac{1}{8} = \frac{1}{2}$ $\frac{4}{8} = \frac{1}{2}$ $\frac{5}{10} = \frac{1}{2}$	$\frac{4}{8} \xrightarrow{5}_{10} \frac{4}{10} \frac{4}{8} \times 5$ 40 = 40
2. $\frac{3}{5} \frac{x^2}{x_2} \frac{8}{10} = \frac{6}{10} \neq \frac{8}{10}$	$\frac{3}{5}$ $\frac{8}{10}$ 3×10 5×10 $30 = \frac{1}{5}$ 40
3. $\frac{3 \times 6}{7 \times 6} \frac{17}{42}$ $\frac{18}{42} \neq \frac{12}{42}$	$\frac{3}{7} \rightarrow \frac{17}{42} 3 \times 4 \partial 7 \times 17$ $1 \partial 6 \neq 119$
4. $\frac{2}{7} \frac{x4}{x4} \frac{12}{28}$ $\frac{8}{28} \pm \frac{12}{28}$	$\frac{\frac{2}{7}}{\frac{12}{28}} \xrightarrow{\frac{12}{28}} 56 \ddagger \frac{3}{8} \frac{7}{8} \frac{7}{8} \frac{12}{8}$

5. 6:8 4:3 $\frac{18}{24} \pm \frac{32}{24}$ 6 $\frac{4}{3} \frac{18}{24} \pm \frac{32}{24}$ $\frac{18}{34} \pm \frac{33}{34}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$5:10\ 15:30 \qquad 5 \times 30\ 10 \times 15 \\ 5 \qquad 15 \qquad 150 = 150 \\ \hline 10 \qquad 30$
7. $\frac{8}{18+2} \frac{20}{45}$ $\frac{20}{45} \frac{20}{45} = \frac{20}{45}$ $\frac{4}{45} \frac{20}{45} = \frac{20}{45} = \frac{20}{45}$ $\frac{9}{x5} \frac{20}{45} = \frac{20}{45}$	$\frac{\frac{8}{18}}{\frac{120}{45}} = \frac{8\times45}{360} = 360$
8. $\frac{6}{14} \stackrel{?}{}_{22}^{9} \frac{9}{22}$ $\frac{3}{7} \stackrel{+}{1} \frac{9}{22}$	$\frac{\frac{6}{14}}{\frac{9}{22}} = \frac{6 \times 22}{132} \frac{14 \times 9}{126}$
9. $\frac{18}{16} \stackrel{2.8}{=} \frac{2.8}{2.5} \stackrel{\times}{=} \frac$	$\frac{18}{16} \frac{2.8}{2.5} 18 \text{ x } 2.5 16 \text{ x } 2.8 \\ 45 \neq 44.8$
$10. \frac{4.5^{10}}{6 \times 10} \frac{7.5}{10} \times \frac{7.0}{10} \frac{7.5}{706} = \frac{7.5}{700}$ $\frac{45}{60} = 15^{5} \frac{3}{4} \times 25^{5} \frac{7.5}{700}$ $\frac{45}{60} = 15^{5} \frac{3}{4} \times 25^{5} \frac{7.5}{700}$	$\frac{4.5}{6} \frac{7.5}{10} \frac{4.5 \times 10}{45} = 45$
$11. \frac{0.35}{0.4 \times 100} \frac{0.7}{0.8} \frac{\times 10}{\times 10} \frac{75}{40} = \frac{35}{40}$ $\frac{35}{40} \frac{7 \times 5}{8 \times 5} \frac{35}{40}$	$\frac{0.35}{0.4} \frac{0.7}{0.8} \qquad \begin{array}{c} 0.35 \times 0.8 & 0.4 \times 0.7 \\ 0.28 & 0.28 \\ \end{array} \begin{array}{c} 0.28 \\ 0.28 \end{array}$

CALP Math

Unit 2: Proportions

LP Math	Unit 2: Proportions
reduce fractions	Cross products
$\frac{18}{11} \frac{18}{11}$	$\frac{\frac{6}{1}}{\frac{11}{3}} \xrightarrow{18}_{11} \frac{6}{7} \times \frac{11}{7} \frac{11}{7} \times \frac{6}{7} \times \frac{11}{7} = \frac{11}{7} \times \frac{6}{7} \times \frac{11}{7} \times \frac{11}{7}$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\frac{2\frac{5}{8}}{3\frac{1}{4}} \xrightarrow{\frac{21}{26}}{\frac{3}{4}} \xrightarrow{\frac{21}{26}}{\frac{3}{4}} \xrightarrow{\frac{21}{26}}{\frac{3}{4}} \xrightarrow{\frac{21}{26}} \xrightarrow{\frac{3}{4}} \xrightarrow{\frac{21}{4}} \xrightarrow{\frac{21}{73}} \xrightarrow{\frac{21}{73}} \xrightarrow{\frac{13}{4}} \xrightarrow{\frac{21}{73}} \xrightarrow{\frac{21}{73}} \xrightarrow{\frac{273}{4}} \xrightarrow{\frac{2}{4}} \xrightarrow{\frac{2}{5}} \xrightarrow{\frac{2}{7}} \xrightarrow{\frac{2}$
$\begin{array}{r} & \text{Product Fraction} \\ \hline x \text{ Product Fraction} \\ 15. \frac{2\frac{3}{10}}{8.05} \frac{1}{4} & 8.05 \stackrel{>}{_{\sim}} 8\frac{1}{20} \\ 15. \frac{2}{10} & \frac{1}{4} & 8.05 \stackrel{>}{_{\sim}} 8\frac{1}{20} \\ 2.9 & 0.9 & 0.9 \stackrel{=}{_{\sim}} 9\frac{1}{10} \\ 2.3 & \frac{9}{10} & 8\frac{1}{20} \times \frac{1}{4} \\ \frac{2.3}{10} \times \frac{9}{10} & \frac{161}{20} \times \frac{1}{4} \\ \frac{207}{100} & \frac{161}{80} \times \frac{1}{80} \end{array}$	$\frac{2\frac{3}{10}}{8.05} \frac{\frac{1}{4}}{0.9} = \frac{2}{10} = 2.3$ $\frac{1}{10} = \frac{1}{4} = 2.3$ $\frac{1}{10} = 2.07 + 2.00125$

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Solving Proportions

Steps for solving a proportion problem using cross-multiplication:

- Step 1: Write the first ratio using the information given.
- **Step 2:** Write the proportion using a letter in place of the missing term. Be sure the order of comparison is the same in both the first and second ratios in your proportion.
- **Step 3:** Write the proportion in fraction form. (Try to simplify the ratio before you do all the calculations.)
- Step 4: Cross-multiply and set the cross products equal to each other.
- Step 5: Divide both sides of the equation by the number with the unknown term.
- Step 6: Check by putting your answer back into the original proportion and crossmultiplying.

Solving for a Missing Term in a Proportion

Example 1

For the ratios below to form a true proportion, the missing term must have a specific value.

What is the value of the missing term?

 $\frac{4}{5} = \frac{x}{30}$ Write the proportion. $30 \div 5 = 6$ Raise the fraction $\frac{4}{5}$ to an equivalent fraction with a denominator of 30 by multiplying the numerator and the denominator by the same number.

$$\frac{4 \times 6}{5 \times 6} = \frac{24}{30}$$
 Multiply the numerator and denominator by 6.

Answer: The missing term of the proportion is 24.

Or use cross-multiplication:

$$\frac{4}{5} = \frac{x}{30}$$
 Write the proportion.

$$4 \cdot 30 = 5 \cdot x$$
 Cross-multiply

$$120 = 5x$$

$$\frac{120}{5} = \frac{5x}{5}$$
 Divide both sides by 5.

$$24 = x$$

Answer: The value of the missing term is 24.

Check the answer by using cross products.

$$\frac{4}{5} = \frac{24}{30} \\ 5 \cdot 24 = 4 \cdot 30 \\ 120 = 120$$

The cross products are the same, so the answer x = 24 is correct.

Example 2

Find the value of the missing term.

$$\frac{3}{x} = \frac{1}{5}$$
Raise the fraction $\frac{1}{5}$ to an equivalent fraction with a numerator that can be

$$\frac{1 \times 3}{5 \times 3} = \frac{3}{15}$$
divided by 3.

Answer: The value for the missing term that will yield a true proportion is 15.

Or cross-multiply:

 $\frac{3}{x} = \frac{1}{5}$ Raise the fraction $\frac{1}{5}$ to an equivalent fraction with a numerator that can $3 \cdot 5 = x \cdot 1$ be divided by 3. $\frac{15}{1} = \frac{1x}{1}$ Then divide. 15 = x

Answer: *x* = 15

Student practice:

1.
$$\frac{2}{3} = \frac{x}{12}$$



$$2. \quad \frac{8}{36} = \frac{10}{x}$$

3.
$$\frac{0.06}{x} = \frac{0.3}{0.4}$$
 Instructor led



$$4. \quad \frac{\frac{1}{4}}{\frac{1}{2}} = \frac{x}{8}$$

Exercise 2.2

Exercise 2.2		1	
Equivalent fractions	Cross products	Equivalent fractions	Cross products
1. $\frac{1}{5} = \frac{x}{25}$ $\frac{1}{5} \times 5 = \frac{x}{35}$ $\frac{5}{35} \times \frac{x}{35} \times \frac{x}{35}$	$\frac{1}{5} = \frac{x}{55}$ $\frac{1.95}{55} = \frac{5.x}{55}$	2. $\frac{16}{x} = \frac{8 \times 2}{3 \times 2}$ $\frac{\frac{16}{16}}{16} = \frac{16}{2}$ $x = 6$	16 - 8 3 8.X 16.3 = 8.X 48 = 8.X 6 - X
3. $\frac{3}{2} = \frac{x}{4}$ $\frac{3x^{2}}{5x^{2}} = \frac{x}{4}$ $\frac{6}{4} = \frac{x}{4} \times = 6$	$3 = \frac{x}{4}$ $3 \cdot 4 = 2 \cdot x$ $\frac{12}{6} = x$	4. $\frac{8}{x} = \frac{4}{5}$ $\frac{8}{5} = \frac{4}{5 \times 2}$ $\frac{8}{5} = \frac{6}{5 \times 2}$ $\frac{8}{5} = \frac{6}{5} \times =10$	$\frac{8}{x} = \frac{4}{5}$ $\frac{8}{x} = \frac{4}{5}$ $\frac{8}{5} = \frac{4}{5}$ $\frac{9}{7} = \frac{4}{5}$ $\frac{4}{7}$
5. $\frac{12}{x} = \frac{16}{4} \div \frac{4}{5}$ $\frac{12}{x} = \frac{16}{4} \div \frac{4}{5}$ $\frac{12}{x} = \frac{4}{5} \times \frac{3}{5}$ $\frac{12}{x} = \frac{12}{5} \times \frac{3}{5}$	$\frac{12}{x} = \frac{16}{4}$ 12x4 = 160X $\frac{48}{16} = \frac{16}{16}$ 3 = X	6. $\frac{9}{x} = \frac{3 \times 3}{4 \times 3}$ $\frac{9}{x} = \frac{9}{12}$ $\frac{12}{x} = 12$	$ \frac{9}{x} = \frac{3}{4} $ $ \frac{9}{x} = \frac{3}{4} $ $ \frac{36}{3} = \frac{3}{3} $ $ \frac{3}{3} = \frac{3}{3} $ $ \frac{3}{12} = \frac{3}{2} $
7. $\frac{28}{x} = \frac{4 \times 7}{7 \times 7}$ $\frac{28}{X} = \frac{28}{49}$ $X = \frac{28}{49}$	$\frac{28}{28} = \frac{4}{7}$ $\frac{28}{28}7 = 4.X$ $\frac{196}{4} = \frac{4}{4}$ $\frac{49}{7} = X$	8. $\frac{21^{\frac{23}{75}} \cdot \frac{3}{25}}{\frac{7}{25}} = \frac{x}{25}$ $\frac{7}{25} = \frac{x}{25}$ $7 = x$	$\frac{21}{75} = \frac{x}{25}$ $\frac{21 \cdot 25}{21 \cdot 25} = 75 \times \frac{525}{75} = \frac{75 \times 1}{75}$ $\frac{7}{7} = x$

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Unit 2: Proportions

Cross prod	ucts only
	10. $\frac{17}{10} = \frac{8.5}{x}$ $\frac{17 \cdot X}{17} = \frac{10 \cdot 8.5}{17}$ $\frac{17 \times 2}{17} = \frac{85}{17}$ X = 5
11. $\frac{2.6}{x} = \frac{13}{7.8}$ $\frac{2.6 \cdot 7.8 = 13 \cdot x}{13}$ $\frac{20 \cdot 28}{13} = \frac{13 \cdot x}{13}$ 1.56 = x	12. $\frac{0.4}{0.9} = \frac{4.8}{x}$ $0.4 \cdot x = 0.9 \cdot 4.8$ $\frac{0.4 \cdot x}{0.4} = \frac{4.32}{0.4}$ $\frac{0.4}{0.4} = 10.8$
$13. \frac{x}{\frac{3}{10}} \frac{\frac{20}{19}}{10} \frac{x}{3} \cdot 1 = \frac{3}{10} \cdot \frac{20}{9}$ $x = \frac{3}{3}$ $X = \frac{3}{3}$ $X = \frac{3}{3}$	14. $\frac{15}{1\frac{2}{3}} = \frac{9}{x}$ $ 5 \cdot x = \frac{2}{3} \cdot 9$ $ 5 \cdot x = \frac{2}{3} \cdot 9$ $ 5 \cdot x = \frac{5}{3} \cdot \frac{7^{3}}{1}$ $\frac{15 \cdot x}{15} = \frac{15}{15}$ X =
$4ecimal 15. \frac{3}{20} = \frac{0.03}{x} \frac{3}{50} = 0.15$ $0.15 \cdot x = 0.1 \cdot 0.03$ $\frac{0.15 \cdot x}{0.15} = \frac{0.003}{0.15}$ $X = 0.02$	$fraction \frac{3}{20} = \frac{0.03}{0.12} 0.12 \frac{1}{100} \frac{3}{20} = \frac{0.03}{100} 0.03 = \frac{3}{100} \frac{3}{20} \times = \frac{1}{10} \frac{3}{100} \frac{3}{100} \frac{1}{100} \frac{3}{20} \times = \frac{1}{10} \frac{3}{100} \frac{3}{100} \frac{1}{100} $

Solving Application Problems with Proportions

Using Proportions to Solve Word Problems

- 1. Read the problem at least twice.
- 2. Decide what you have to find (the missing term) and assign a letter to represent it.
- 3. Set up a proportion using the information given.
- 4. Solve the proportion.
- 5. Write the answer in sentence form, including the appropriate units of measure.

Example 1

At the rate of 5 articles for 20 cents, find the cost of 4 articles.

Solution:

The question asks us to find the cost. Use the letter C to represent cost.

 $\frac{5 \text{ articles}}{20 \notin} = \frac{4 \text{ articles}}{C}$ Set up a proportion.

Note: The top and bottom terms must correspond (represent the same things). In this example, the top terms represent the number of articles, and the bottoms terms represent cost.

$$\frac{5}{20} = \frac{4}{C}$$

$$5 \times C = 4 \times 20$$
Cross-multiply.
$$5C = 80$$

$$\frac{5C}{5} = \frac{80}{5}$$
Divide both sides by 5 to find the unknown value.
$$C = 16$$
The value of C is 16. Write the answer in sentence form, including the proper units.

Answer: 4 articles cost 16 cents.

V1.18

Student practice:

1. A grocery store sells 3 boxes of cereal for \$11.50. At this rate, how much would 9 boxes of cereal cost?



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2. John can drive 150 kilometres in 2 hours. At this rate, how long would it take him to drive 375 kilometres?

Exercise 2.3

Solve each of the following problems. Round the answers to the nearest tenth as necessary.

1. A recipe uses 3 pounds of hamburger to make a casserole large enough to feed 13 people. Using the same recipe, how many people could be fed with 9 pounds of hamburger?

$$\frac{3pounds}{13poople} = \frac{9pounds}{X} \qquad \frac{3}{13} = \frac{9}{X} \qquad 3 \circ X = 13 \circ 9$$

$$\frac{3pounds}{13poople} = \frac{9pounds}{X} \qquad \frac{3}{13} = \frac{9}{X} \qquad 3 \circ X = 13 \circ 9$$

$$\frac{3pounds}{13poople} = \frac{117}{12} \qquad \frac{3x}{3poople} = \frac{117}{3} \qquad x = 39$$
2. Joe can run 100 metres in 12 seconds. If he maintains the same speed, how far could he run in 36 seconds?
$$\frac{100m}{12s} = \frac{X}{36s} \qquad \frac{100}{12} = \frac{X}{36}$$

$$\frac{100 \circ 36}{12} = \frac{12}{12} \qquad \frac{300}{12} = \frac{12}{12} \qquad \frac{30}{12} = \frac{10}{12} \qquad \frac{30}{12} = \frac{10}{12} \qquad \frac{30}{12} = \frac{10}{12} \qquad \frac{30}{12} = \frac{10}{12} \qquad \frac{10}{12} = \frac{10}{12} \qquad \frac{10}{12} = \frac{10}{12} \qquad \frac{10}{12} = \frac{10}{12} \qquad \frac{10}{12} \qquad \frac{10}{12} = \frac{10}{12} \qquad \frac{10}$$

3. A large container of soap cost \$9 for 12 litres. What could you expect to pay for 4 litres?

$$\frac{\$}{12L} = \frac{X}{4L} \qquad \begin{array}{l} 9.4 = 12.x \\ 3.6 = 12x \\ 12 \\ 12 \\ \end{array}$$
You would pay $\$ 3.00$ for 4/itres of soap.

4. Gertrude walked 9 blocks in 15 minutes. At the same rate, how long will it take her to walk 18 blocks?

$$\frac{9b/ocks}{15 \text{ minutes}} = \frac{18b/ocks}{X} \qquad \frac{9 \cdot x}{9 \cdot x} = \frac{18}{9} \frac{18}{7} \frac{18}{7} \frac{18}{7} = \frac{18}{9} \frac{18}{7} \frac{18}{7$$

5. A truck travelled 250 kilometres in 5 hours. At this speed, how long would it take to complete a trip of 650 kilometres?

$$\frac{250 \text{ km}}{5 \text{ hours}} = \frac{650 \text{ km}}{X} \qquad \frac{5.650}{3250} = \frac{250 \times}{250}$$

$$\frac{3250}{250} = \frac{250 \times}{250}$$

$$\frac{3250}{13} = X$$
The Truck will take 13 hours to travel 650 km.

6. If the scale of distance of 1 centimetre on a map represents an actual distance of 10 kilometres, what actual distance does a scale distance of 5.7 centimetres represent?

$$\frac{1 \text{ cm}}{10 \text{ km}} = \frac{5.7 \text{ cm}}{x} \qquad 1.0 \text{ cm} = 5.7$$

- Sircm on the map will be S7kminactual distance.
- 7. The directions on the lawn fertilizer say to spread 1.7 kilograms over 100 square metres of lawn. How much fertilizer is needed for a lawn measuring 130 square metres?

$$\frac{1.7 \text{ kg}}{100 \text{ m}^2} = \frac{X}{130 \text{ m}^2}$$

$$\frac{1.7 \cdot 130}{221} = 100 \cdot X$$

$$\frac{221}{100} = \frac{100 \times 100}{100}$$

$$2.21 = X$$

$$-.21 \text{ kilograms of Fertilizer is needed.}$$

8. The taxes on a property valued at \$300 000 are \$5 000. At the same rate of taxation, what would the taxes be on the smaller lot down the street that is valued at \$240 000?

$$\frac{4300000}{$\times 5000} = \frac{240000}{$\times 5000} = \frac{300000}{$\times 5000} = \frac{300000}{$\times 5000} = \frac{1030000000}{$\times 5000} = \frac{1030000000}{$\times 5000} = \frac{103000000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{103000000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{10300000000}{$\times 5000} = \frac{103000000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{103000000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{1030000}{$\times 5000} = \frac{1030000}{$\times 5000} = \frac{10300000}{$\times 5000} = \frac{1030000}{$\times 5000} = \frac{103000}{$\times 5000} = \frac{103000}{$\times 5000} = \frac{1030000}{$\times 5000} = \frac{103000}{$\times 5000} = \frac{1030000}{$\times 5000} = \frac{103000}{$\times 5000} = \frac{100000}{$\times 5000} = \frac{100000}{$\times 5000} = \frac{100000}{$\times 5000}$$

- 9. The class spends 6 hours a week on math and 8 hours on English. At this rate, if the class spent 10½ hours on math, how much time would be spent on English?
- $\frac{6h \text{ math}}{8h \text{ English}} = \frac{10 \frac{1}{2} hours}{X} \quad 6 \times = 8 \cdot 10 \frac{1}{2}$ $\frac{6x}{8h \text{ English}} = \frac{10 \frac{1}{2} hours}{6x} \quad 6 \times = 8 \cdot 10 \frac{1}{2}$ $\frac{6x}{84} = \frac{21}{84}$ The class would spend $\frac{6x}{6} = \frac{84}{6}$ $\frac{6x}{6} = \frac{84}{6}$
- 10. At 4 p.m., Glen's shadow is 2.15 metres long. His height is 1.85 metres. A tree nearby has a shadow that is 7.2 metres long. How tall is the tree? Round your answer to the nearest hundredth of a metre.

$$\frac{2.15m \text{ shadow}}{1.85m \text{ height}} = \frac{7.2m}{\times} \qquad \begin{array}{l} 2.15 \cdot x = 1.85 \cdot 7.2m \\ 2.15 \cdot x = 13.32 \\ 2.15 \end{array} \qquad \begin{array}{l} 2.15 \times z = 13.32 \\ 2.15 \end{array} \qquad \begin{array}{l} 2.15 \times z = 13.32 \\ 2.15 \end{array} \qquad \begin{array}{l} 2.15 \times z = 13.32 \\ 2.15 \end{array} \qquad \begin{array}{l} 2.15 \times z = 13.32 \\ 2.15 \end{array} \qquad \begin{array}{l} 2.15 \times z = 13.32 \\ 2.15 \end{array} \qquad \begin{array}{l} 2.15 \times z = 13.32 \\ 2.15 \times z = 6.20 \end{array}$$
The tree is 6.2 metres tall.

Unit 3: Percent

Think about...

When we buy something at a store, we always pay more than the posted price. If we buy something that costs \$1.00, we pay \$0.05 more in tax (GST), so the final cost is \$1.05. In Canada, we pay 5% GST on all goods.

Percent is a ratio that has many applications—interest rates, discounts, sales tax, and marks are all expressed as a percent.

- Percent means "out of a hundred."
- ♦ 75% means $\frac{75}{100}$ or 0.75

Percent as a Decimal

Percent can be written in decimal form by dividing by 100 and dropping the % sign.

• Dividing by 100 is the same as moving the decimal two places to the left.

Decimals can be written in % form by multiplying by 100 (the same as moving the decimal two places to the right) and adding the percent sign.

• 0.75 = 75%

Example 1

Write 20% as a decimal.

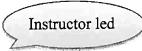
 $20\% = 20 \div 100 = 0.2$ Two decimal places means hundredths.

Example 2

Write 0.4 as a percent.

 $0.4 \times 100 = 40$ Multiply by 100 or move the decimal two places to the right. = 40% Drop the decimal point and add the percent sign.

Student practice:





- 1. Write 45% as a decimal.
- 2. Write 0.234 as a percent.

Exercise 3.1

- Write each of the following decimal numbers as a percent. 1.
- move decimal 2 places c. 0.04 × 100 4 % a. 0.56 × 100 b. 0.6 × /00 0.60 0.046 40% 56% 60°/0 0.855 85.5% f. e. 0,<u>6</u>25 d. 0.21 62.5% 210/0 i. 1.23, 12.3% h. 2<u>3</u>5, 235% g. 1.702 170%

Write each of the following percents in decimal form. 2.

a. 24% = 100 24 = 100 = 0.24	b. 33% 33.% 0,33	c. (15% 0.05
d. <u>16</u> .7% 0.167	e. 120% 1.2	f. 299% J
g. 44% 0.44	h. 125%	i. <u>87</u> .5% 0,875

Percent and Fractions

Example 1

There are two ways to write a fraction as a percent.

Write ³/₄ as a percent.

1. Change the fraction to a decimal by dividing. Then move the decimal two places to the right by multiplying by 100.

$$\frac{3}{4} = 3 \div 4 = 0.75$$
$$0.75 \times 100 = 75\%$$

Or

2. First write the fraction as a proportion. Remember that percent (%) is always out of 100.

 $\frac{3}{4} = \frac{n}{100}$ $3 \cdot 100 = 4n$ Then cross-multiply and divide. $\frac{300}{4} = \frac{4n}{4}$ 75 = n $\frac{3}{4} = 75\%$

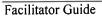
Example 2

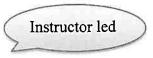
Write 20% as a fraction.

20 _ 1	To write 20% as a fraction, put 20 over 100 and drop the % sign.
$\frac{100}{100} = \frac{1}{5}$	Then reduce the fraction to lowest terms.

Student practice:

- 1. Write 18% as a fraction.
- 2. Write $\frac{3}{5}$ as a percent.
- 3. Write 35% as a fraction and a decimal.







Exercise 3.2

Write each fraction as a percent. Round your answer to one decimal place when necessary. 1.

a.
$$\frac{7}{10_{x10}} = \frac{70}{10_{x10}}$$

b. $\frac{2}{5} \times \frac{20}{5}$
 $\frac{40}{100} = \frac{40^{2}}{100}$
 $\frac{70^{2}}{100}$
 $\frac{70^{2}}{100}$
 $\frac{70^{2}}{100}$
b. $\frac{2 \times 20}{5 \times 30}$
 $\frac{40}{100} = \frac{40^{2}}{100}$
 $\frac{25}{100} = \frac{25^{2}}{100}$
 $\frac{25}{100} = \frac{25^{2}}{100}$
 $\frac{25}{100} = \frac{25^{2}}{100}$
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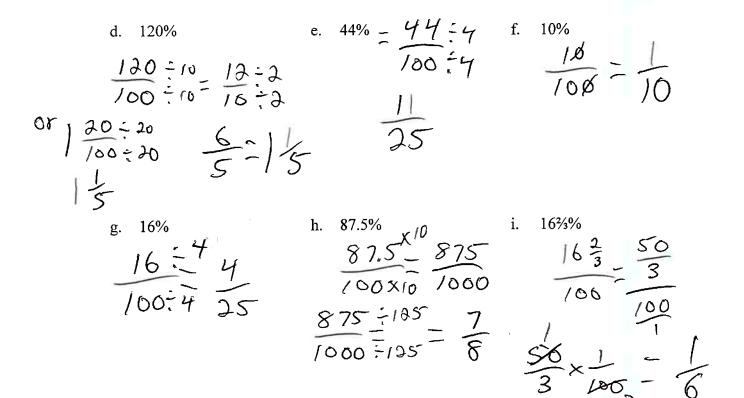
.

d.
$$\frac{1}{2} \underset{x \leq 0}{\overset{x \leq 0}{\longrightarrow}} = \frac{50}{700}$$
 e. $\frac{3}{8}$ f. $\frac{4}{9} = \frac{x}{700}$ $\frac{9x}{9x} = \frac{4.100}{900}$
or $\frac{50\%}{9}$ $\frac{9}{8} / \frac{3.000}{3.000} = 0.375$ $\frac{9x}{9} = \frac{400}{9}$
 $\frac{10}{9} \times \frac{244}{9} = \frac{3}{7.5\%}$ $x = 44.4\%$
g. $\frac{7}{8} \times \frac{7.000}{50}$ h. $\frac{3}{2} = \frac{x}{700}$ i. $\frac{2}{3} = \frac{x}{700}$
or $\frac{60}{50}$ $\frac{2x}{70} = \frac{300}{3}$ $\frac{200}{3} = \frac{3x}{3}$
 $\frac{7}{8} = \frac{700}{100}$ $\frac{40}{70} \times = 150\%$ 66.7% $\times = 87.5\%$

Write each percent as a fraction or mixed number and reduce to lowest terms. 2.

a.
$$24\%$$

 $j = \frac{24\%}{100 \div 7} \div \frac{6}{25} \qquad \frac{33}{100}$
b. 33%
c. 6%
 $j = \frac{3}{100} \div 2 \div \frac{3}{50}$



3. Extra Practice: Fractions, Decimals, and Percent

Complete the table below by filling in the empty blocks.

	Fraction	Decimal	Percent
a.	$\frac{1}{4}$	4/1.00 80,25 20 30 0	$\begin{array}{c} 0.25 \times 100 \\ 35^{\circ} \\ -25^{\circ} \\ -25^{\circ} \\ -25^{\circ} \\ +25^{\circ} \\ +25^{\circ}$
b.	5=5=1 10=5=2	0.5	0.50, 50%
с.	75 = 25 3 100 = 25 4	75% 0.75	75%

-	Fraction	Decimal	Percent
đ.	$\frac{1}{8}$	8/1.000 767 767	0,125 12.5%
e.	$\frac{375 \div 25}{1000 \div 25 =} \frac{15}{40}$ $\frac{15 \div 5}{40 \div 5 =} \frac{3}{8}$	0.375	0.375 37.5%
f.	62:231 100:2550	0.62	62%

Solving Problems with Percent: Part I

Percent Problems

You can use the following formula to solve all percent problems:

$$\frac{\text{is (part)}}{\text{of (whole)}} = \frac{\%}{100}$$

Example 1

Find 30% of 40.

Before a percent problem can be solved, the percent must be expressed as a decimal or a fraction, or you can use the above formula.

30% of 40	or	is(part) = percent
$= 0.30 \times 40$		of (whole) 100
= 12		$\frac{x}{40} = \frac{30}{100}$
		$100 \bullet x = 30 \bullet 40$
		100x = 1200
		$\frac{100x}{100} = \frac{1200}{100}$
		x = 12

Answer: 30% of 40 is 12.

Example 2

65% of a number is 130. What is the number? Let n represent the unknown number.

65% of n is 130	or	is (part) percent
0.65 <i>n</i> = 130		of (whole) 100
$\frac{0.65n}{0.65} = \frac{130}{0.65}$		$\frac{130}{n} = \frac{65}{100}$
n = 200		$130 \bullet 100 = 65 \bullet n$
		$\frac{13000}{65} = \frac{65n}{65}$
		200 = n

Answer: 65% of 200 is 130.

Example 3

What percent of 50 is 75? Let n represent the unknown percent.

n% of 50 is 75 0.01*n* × 50 = 75 ← *n*% = *n* hundredths or 0.01*n* 0.5*n* = 75 $\frac{0.5n}{0.5} = \frac{75}{0.5}$ *n* = 150 or 150%

Or cross-multiply and divide:

$$\frac{75}{50} = \frac{\%}{100}$$
$$\frac{75}{50} = \frac{n}{100}$$
$$75 \cdot 100 = 50n$$
$$\frac{7500}{50} = n$$
$$150 = n$$

Answer: 150% of 50 is 75.

Student practice:

1. 20% of what number is 12?

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2. Tim wrote a test and scored 80%. If the test had 20 questions and each question was worth 1 mark, how many questions did Tim answer correctly?

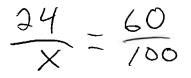
3. Stores offer discounts to attract customers. One store is offering a 40% discount on all their appliances. If a refrigerator regularly sells for \$1 200, what would the sale price be?

Exercise 3.3

1. Find 25% of 40.

$$\frac{15}{0f} = \frac{0}{100}$$
or
$$\frac{Part}{100} = \frac{0}{100}$$

2. 60% of what number is 24?



0/0

3. What percent of 20 is 16?

$$\frac{16}{20} = \frac{x}{100}$$

4. 150% of what number is 30?

$$\frac{30}{X} = \frac{150}{100}$$

$$\frac{x}{16} = \frac{25}{100} \qquad \frac{100x}{100} = \frac{1000}{100} \\ x = 10$$

$$\frac{24 \cdot 100}{60} = \frac{60 \cdot x}{60}$$

$$\frac{2400}{60} = \frac{60x}{60}$$

$$\frac{40}{60} = x$$

$$16.100 = 20.X$$

$$\frac{1600}{20} - \frac{30}{20}$$
$$80 = X$$

$$30.100 = 150.x$$

 $\frac{3000}{150} = \frac{150.x}{150}$
 $\frac{150}{150} = \frac{150.x}{150}$
 $20 = X$

5. Find 10% of \$460.

$$\frac{x}{460} = \frac{10}{100}$$

$$100x = 460.10$$

 $\frac{100x}{400} = \frac{4600}{100}$
 $x = 4600$
 $x = 4600$

7

6. 0.5% of what number is 5?

$$\frac{5}{x} = \frac{0.5}{100}$$

$$5.100 = 0.5 \times$$

$$500 = 0.5 \times$$

$$0.5 = 0.5 \times$$

$$1000 = X$$

$$3500 = 125 \times$$

$$125 = 125 \times$$

$$125 = 200 = 125 \times$$

 $\frac{25}{125} = \frac{x}{100}$

7.

What percent of 125 is 25?

8. 75% of 12 is what number?

$$\frac{X}{12} = \frac{75}{100} \qquad \frac{100 \times}{100} = \frac{900}{100} \\ X = 9$$

9. What is 16% of 34?

$$\frac{X}{34} = \frac{16}{100} \qquad \frac{100 \times = 544}{100} \qquad \frac{100 \times = 54}{100} \qquad \frac{100 \times =$$

10. What is 90% of 75?

$$\frac{X}{75} = \frac{90}{100} \qquad \frac{100x}{100} = \frac{6750}{100} \\ X = 67.5$$

-

11. The seller pays a 5% commission for selling a house. What is the commission for the sale of a house valued at \$110 000?

$$\frac{X}{110\ 000} = \frac{5}{100} \qquad \frac{100 \times 2}{100} = \frac{550\ 000}{100}$$

$$X = 5500$$
The commission for selling the house is
$$\frac{85500}{12}$$
12. Calculate the sale price for a camera regularly priced at \$150, on sale at 20% off.

$$\frac{X}{150} = \frac{20}{100} \qquad \frac{100x}{100} = \frac{3000}{100} \qquad \frac{\cos t - discount = total}{150 - 30}$$

The sale price of the camera is 120

13. Josephine paid \$150 for a camera that was on sale for 25% off. What was the regular price of the camera? Since she got 25% off she paid

$$\frac{150}{x} = \frac{75}{100} \qquad \frac{75}{75} \qquad \frac{75}{75} = \frac{15000}{75} \qquad X = \frac{15000}{75}$$
The camera's regular price is \$200.

14. In telethons and other fundraising events, records show that only about 80% of the money pledged is actually collected. Local telethon organizers need to raise \$12 000. To raise \$12 000, their goal for pledges should be what amount?

$$\frac{12000}{X} = \frac{80}{100} \quad \frac{80x}{80} = \frac{1200000}{80}$$

$$X = 15000$$
Their goal should be to raise \$15000.

Solving Problems with Percent: Part II

Problems that ask you to find the percent of increase or decrease

Solving this type of problem often involve twos steps:

- Step 1: Find the amount of change (either increase or decrease) by finding the difference between the two amounts given. Subtract to find the difference.
- Step 2: Find the percentage of increase or decrease. Always compare the change (the amount of increase or decrease) to the amount before the change (the original amount) using this proportion:

 $\frac{\text{amount of change or difference}}{\text{original amount}} = \frac{\% \text{ increase or decrease}}{100}$

Example 1

The rent went from \$375 a month to \$427.50 a month. By what percent did the rent increase?

Step 1: Find the change (the amount of increase) by finding the difference between the amounts.

427.50 - 375 = 52.50. The amount of increase is \$52.50.

Step 2: Find the percent of increase.

The amount of increase is \$52.50. The original amount (the amount before the increase) is \$375.

$$\frac{\text{difference}}{\text{original}} = \frac{\text{percent}}{100}$$
$$\frac{52.50}{375} = \frac{n}{100}$$
$$5250 = 375n$$
$$\frac{5250}{375} = \frac{375n}{375}$$
$$14 = n$$

Answer: The rent increased by 14%.

Example 2

The hours of operation of the Tim Horton's at the college were reduced from 35 hours a week to 28 hours a week. By what percent did the operating hours decrease?

Step 1: Find the amount change (a decrease) by finding the difference between the amounts.

35 hours - 28 hours = 7 hoursThe amount of decrease is 7 hours.

Step 2: Find the percent decrease.

The decrease is 7 hours. The original amount is 35 hours.

What percent is 7 of 35?

$$\frac{\text{difference}}{\text{original}} = \frac{\text{percent}}{100}$$
$$\frac{7}{35} = \frac{\%}{100}$$
$$\frac{7}{35} = \frac{n}{100}$$
$$7 \cdot 100 = 35n$$
$$20 = n$$

Answer: The operating hours decreased by 20%.

Problems that require solving for price plus GST

Price + GST = Total Price (Note: GST is 5%.)

Example 3

Jane bought a pair of pants costing \$59.99. At the checkout counter, she is charged the price plus GST (5%). How much did Jane pay for the pants?

Step 1: Calculate 5% of the cost to find the GST.

$$\frac{x}{59.99} = \frac{5}{100}$$

$$100x = 5 \cdot 59.99$$

$$\frac{100x}{100} = \frac{299.95}{100}$$

$$x = 2.9995$$

$$x = 3$$

5% of the cost (the GST) is \$3.

Step 2: Add the GST to the initial price to find the total cost.

\$59.99 + \$3.00 = \$62.99

Answer: Jane paid \$62.99 for the pants.

Student practice:

1. The cost of hourly parking went from \$9 per day to \$12 per day. By what percent did the parking fees increase?



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-		1.0		

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2. Jamal bought an iPhone for \$730.00. Find the amount of GST and the total cost of the iPhone.

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Exercise 3.4

Jennifer's wage recently went from \$10.00 an hour to \$10.50 an hour. By what percent did her wages increase?

$$\frac{\text{difference}}{\text{Original}} = \frac{90}{100} \qquad \frac{-10.00}{0.50} \qquad \frac{0.50}{10.00} = \frac{100}{100} \qquad \frac{1000}{100} = \frac{100}{100} \qquad \frac{1000}{10} = \frac{50}{100} \qquad \frac{1000}{100} = \frac{1000}{100} \qquad \frac$$

.

2. The enrolment in the afternoon bowling league went from 40 bowlers to 50 bowlers for the spring session. By what percent did the number of bowlers increase?

$$50 - 40 = 10$$

$$\frac{10}{40} = \frac{x}{100} \qquad \frac{40x}{40} = \frac{1000}{40}$$

$$x = 25$$
The number of bow/ers increased by 25%.

3. A regular toilet uses 20 litres of water per flush. A new low-flow toilet uses only 6 litres per flush. What is the percent savings of water per flush if the new toilet is used?

$$\frac{14}{20} = \frac{x}{100} \qquad \frac{20 \times 1400}{20} \qquad \frac{14}{20} = \frac{1400}{20} \qquad \frac$$

4. Sixteen litres of raw strawberries only produced 13.5 litres of cooked strawberries. By what percent did the amount of strawberries shrink? 16 - 13, 5 = 2, 5

$$\frac{2.5}{16} = \frac{x}{100} \qquad 16x = 250$$

$$\frac{16x}{16} = \frac{350}{16}$$

$$\frac{16x}{16} = \frac{350}{16}$$

$$X = 15.6\%$$
The amount of strawberries shrak 15.6%.

5. A car dealership gives a special deal if the customer does not have a trade-in and pays cash. The dealer will only charge \$10 650 for a car listed at \$12 000. What is the percent savings in this deal?

$$\frac{1350}{12000} = \frac{X}{100} = \frac{10000 - 10000}{12000 \times 13500} = \frac{135000}{12000}$$

$$\frac{12000 \times 135000}{12000 \times 12000} = \frac{135000}{12000}$$

$$\frac{12000 \times 13500}{12000}$$

$$\frac{12000 \times 13500}{12000}$$

Facilitator Guide

b.

- 6. A watch is regularly priced at \$90.00. It is on sale for 10% off.
 - a. How much is the discount?

$$\frac{X}{90} = \frac{10}{100} \qquad \frac{100 \times = 900}{100}$$
What is the sale price?

$$\frac{90}{-9} \qquad \text{The Sale price is $\$81$.}$$

7. Sylvia receives a weekly salary of \$280.00 plus a commission of 8% on all the sales she makes over \$2 000.00. Last week, she sold \$5 600.00 worth of merchandise. How much money did she make?
 ∑6 00 - 2000 = 3600

$$\frac{x}{3600} = \frac{8}{100} \qquad \frac{100 x}{100} = \frac{28800}{100}$$

$$x = 288 \text{ Commission}$$
Salary + commission = total earnings
$$\frac{100 x}{100} = \frac{100}{100}$$

$$\frac{100 x}{100} = 288 = 288 \text{ Commission}$$

$$\frac{100 x}{100} = 288 = 100 \text{ Commission}$$

$$\frac{100 x}{100} = 288 = 288 \text{ Commission}$$

8. For each item in the table below, find the GST (5%), then calculate the total cost.

	Item	Cost	GST (5%)	Total Cost
a.	T-shirt	\$14.99	$\frac{\times}{14.99} = \frac{5}{100}$ $\frac{100 \times 7}{100} = 74.95$ $\frac{\times}{200075}$	14.99+0.75 \$15.74
b.	New car	\$27 890.00	$\frac{x}{27890} = \frac{5}{100}$ $\frac{100x}{100x} = 139450$ $\frac{x}{1394.50}$	27890+1394.50 \$29284.50
с.	60" flat-screen TV	\$699.00	$\frac{x}{699} = \frac{5}{100}$ $\frac{699}{100} = 3495$ $x = ^{$3}4.95$	699+34.95 \$733.95

Post-Module Assessment and Answer Key

Post-Module Assessment

Now that you have completed this module, reassess what you can do against this checklist:

	In this module, I will learn how to	I can't do this	I can do this with help	I can do this!
1.	Work with ratios and rates			
2.	Solve proportions			
3.	Work with percent			
4.	Change between fractions, decimals, and percents			
5.	Solve application problems with proportions and percents			

Answer Key

Exercise 1.1

1. a. $\frac{3}{1}$ or 3:1 b. $\frac{4}{20} = \frac{1}{5}$ or 1:5 c. $\frac{15}{60} = \frac{1}{4}$ or 1:4 d. $\frac{30}{120} = \frac{1}{4}$ or 1:4 e. $\frac{36}{18} = \frac{2}{1}$ or 2:1 2. a. $\frac{160}{20} = \frac{8}{1}$ or 8:1 b. $\frac{120}{180} = \frac{2}{3}$ or 2:3 c. $\frac{15}{45} = \frac{1}{3}$ or 1:3 d. $\frac{0.18}{0.12} = \frac{3}{2}$ or 3:2 e. $\frac{20}{180} = \frac{1}{9}$ or 1:9

Exercise 1.2

1.	95¢:1 dozen	2.	100 km:1 h
3.	18:9 = 2 m:\$1	4.	18 km:1 L
5.	52 cars:1 min	6.	1 500 revolutions:1 min
7.	540:10 = 54 words:1 min	8.	20:5 = 4 tbsp:1 kg
9.	$80:10 = 8\phi:1$ g	10.	\$3.60:3 = \$1.20:1 light bulb
11.	1 000:4 = 250 km:1 h	12.	274:50 = 5.5 clocks:1 home
13.	732:10 = 73.2 beats:1 min	14.	450:25 = 18 km:1 L

15. 45:3 = 15 km/h

Exercise 2.1

1. =	2. ≠	3. ≠	4 . ≠	5. ≠
6. =	7. =	8. ≠	9 . ≠	10. =
11. =	12. =	13. =	14. =	15. <i>≠</i>

Exercise 2.2

1. $x = 5$	2. $x = 6$	3. $x = 6$	4. $x = 10$	5. $x = 3$
	7. $x = 49$			
11. $x = 1.56$	12. $x = 10.8$	13. $x = \frac{2}{3}$	14. $x = 1$	15. $x = 0.02$ or $\frac{1}{50}$

Exercise 2.3

1.	You could feed 39 people.	2.	Joe could run 300 metres.
3.	You could expect to pay \$3.	4.	It will take her 30 minutes.
5.	It would take 13 hours.	6.	It represents 57 kilometres.
7.	You would need 2.21 kilograms of fertilizer.	8.	The taxes would be \$4000.
9.	14 hours would be spent on English.	10.	The tree is 6.2 metres tall.

Exercise 3.1

1.	a.	56%	b.	60%	c.	4%	d.	21%	e.	62.5%
	f.	85.5%	g.	170%	h.	235%	i.	123%		
2.	a.	0.24	b.	0.33	c.	0.05	d.	0.167	e.	1.2
	f.	2	g.	0.44	h.	1.25	i.	0.875		

Exercise 3.2

1.	a.	70%	b.	40%	c.	25%		d. 50%	e. 37.5%
	f.	$44\frac{4}{9}\% \text{ or } 44$	1.4%	g.	71.4%		h.	150% i.	$66\frac{2}{3}\% \text{ or } 66.7\%$
2.	a.	$\frac{6}{25}$	b.	$\frac{33}{100}$	c.	$\frac{3}{50}$		d. $\frac{6}{5}$ or $1\frac{1}{5}$	e. $\frac{11}{25}$
	f.	$\frac{1}{10}$	g.	$\frac{4}{25}$	h.	$\frac{7}{8}$		i. $\frac{1}{6}$	

3.

	Fraction	Decimal	Percent
a.	$\frac{1}{4}$	0.25	25%
b.	$\frac{1}{2}$	0.5	50%
c.	$\frac{3}{4}$	0.75	75%
d.	$\frac{1}{8}$	0.125	12.5%
е.	$\frac{3}{8}$	0.375	37.5%
f.	$\frac{31}{50}$	0.62	62%

Exercise 3.3

1.	10	2.	40	3.	80%	4.	20	5.	\$46
6.	1000	7.	20%	8.	9	9.	5.4 or 5.44	10.	67.5
11.	\$5 500	12.	\$120	13.	\$200	14.	\$15 000		

Exercise 3.4

- 1. Jennifer's wages increase by 5%.
- 2. The number of bowlers increased by 25%.
- 3. There is a 70% savings of water per flush.
- 4. The amount of strawberries shrunk by 15.625%.
- 5. The customer would save 11.25%.
- 6. a. The discount is \$9.
 - b. The sale price is \$81.
- 7. Sylvia made \$568.

8.	a.	GST = \$0.75	b.	GST = \$1 394.50	c.	GST = \$34.95
		Total Cost = \$15.74		Total Cost = \$29 284.50		Total Cost = \$733.95